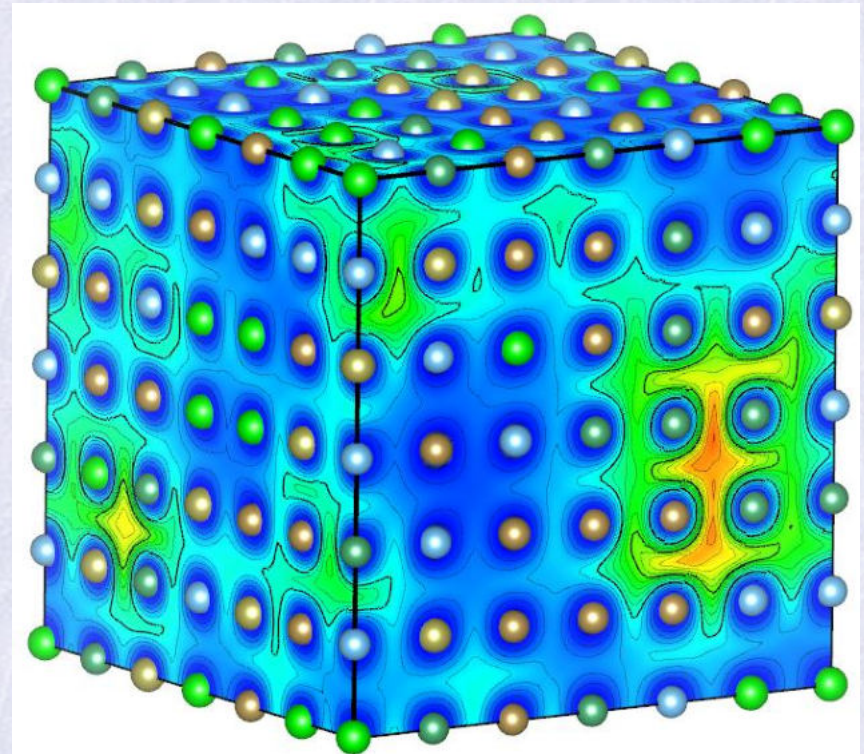


# Positron annihilation study of high entropy alloys



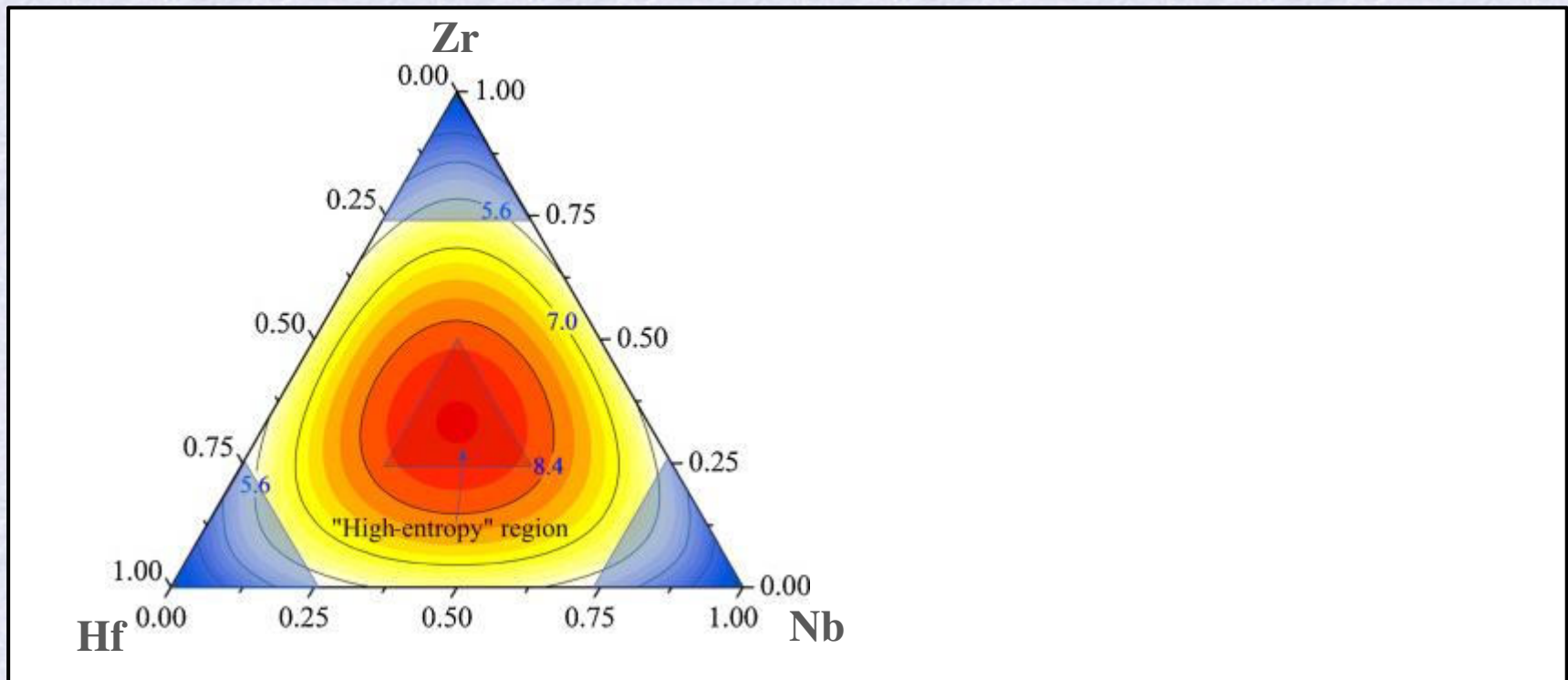
J. Čížek, O. Melikhova, D. Starý, T. Vlasák, F. Lukáč

*Faculty of Mathematics and Physics, Charles University, Prague,  
Czech Republic*



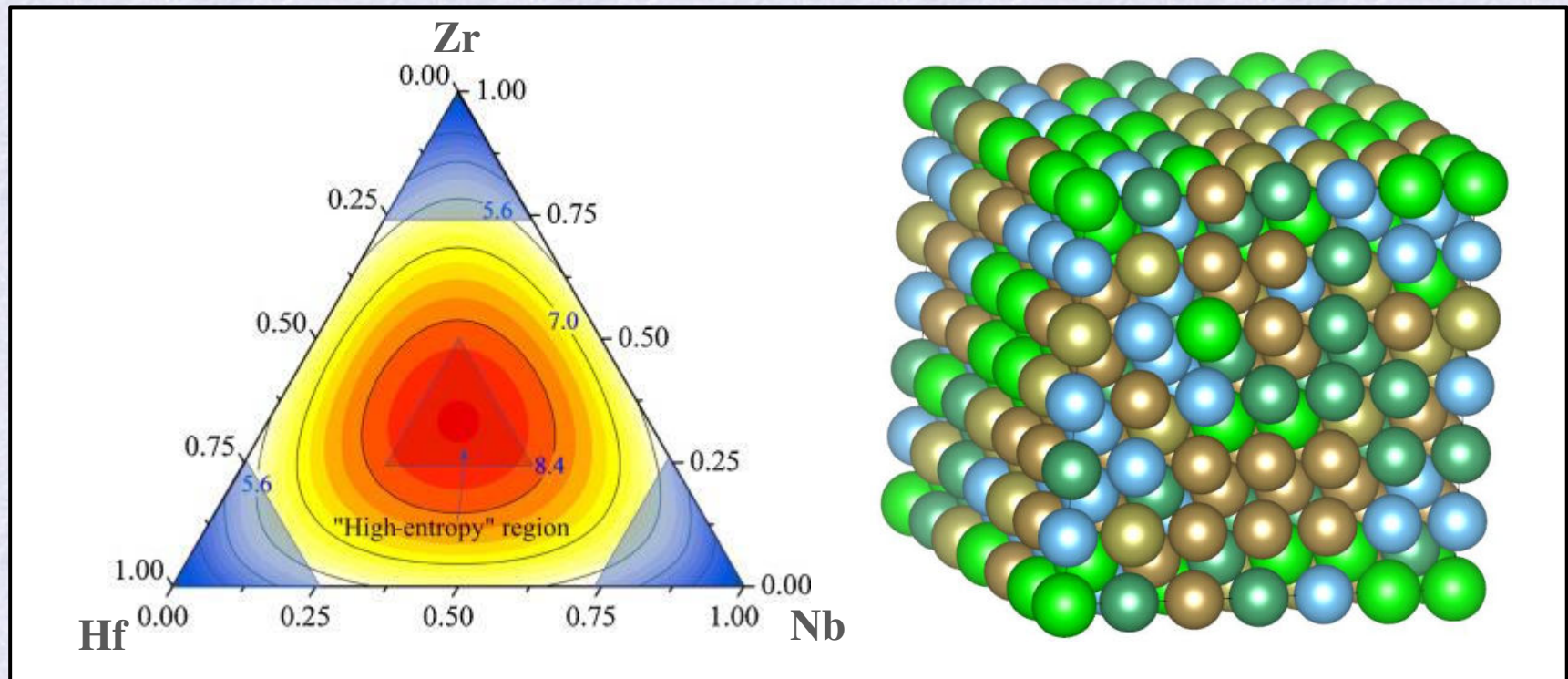
# High entropy alloys (HEAs)

- Alloys consisting of at least 5 alloying elements with concentrations 5-35 at.%
- Complex concentrated alloys
- Exploring of central regions of multi-element equilibrium phase diagrams



# High entropy alloys (HEAs)

- cubic structure (fcc or bcc)
- lattice sites randomly occupied by alloying elements
- favorable mechanical properties in a broad temperature range
- resistance against radiation damage
- high hydrogen storage capacity



# Thermodynamics of HEAs

- Alloys consisting of at least 5 alloying elements with concentrations 5 -35 at.%
- Alloys with configurational entropy of mixing  $S^{SS} \geq 1.6 R$

## random solid solution (SS)

configurational entropy of mixing:  $S^{SS} = -R \sum_{i=1}^N c_i \ln c_i$

concentration  
of *i*-th element

equimolar concentration of *N* elements:  $S^{SS} = R \ln N$

e.g. 5 element alloy, equimolar concentration:  $S^{SS} \approx 1.61R$

universal gas constant  
 $R = 8.314 \text{ JK}^{-1}\text{mol}^{-1}$

# Thermodynamics of HEAs

- Alloys consisting of at least 5 alloying elements with concentrations 5 -35 at.%
- $-TS^{SS} < H^{IM} \Rightarrow$  random SS is thermodynamically stable state of HEA

## random solid solution (SS)

configurational entropy of mixing:  $S^{SS} = -R \sum_i c_i \ln c_i$

Gibbs energy:  $G^{SS} = H^{SS} - TS^{SS} \approx -TS^{SS}$

*excess enthalpy of mixing*  $\nearrow$   $H^{SS}$   $\nwarrow$   $T$   $\nwarrow$   $S^{SS}$  *configurational entropy of mixing*

ideal random SS:  $H^{SS} \approx 0$

$$G^{SS} < G^{IM}$$

## ordered intermetallics phase (IM)

Gibbs energy:  $G^{IM} = H^{IM} - TS^{IM} \approx H^{IM} < 0$

perfectly ordered IM:  $S^{IM} \approx 0$

# Four “core effects” of HEAs

1. high entropy ( $S^{SS} \geq 1.6 R$ ) ← true

- random SS might be energetically more favorable than competing IM phases

J.W. Yeh, et al. Adv. Eng. Mater. 6 (2004) 299

2. lattice distortions

- several lattice distortion due to different atom sizes

L.R. Owen, N.G. Jones, Scripta Mater. 187 (2020) 428

3. sluggish diffusion ← ???? doubtful

- diffusion in HEAs is slower than in conventional alloys

J.W. Yeh, et al. Adv. Eng. Mater. 6 (2004) 299

4. ‘cocktail effect’ ← obvious

- HEA properties may significantly differ from superposition of constituent properties

S.Ranganathan, Curr. Sci. 85 (2003) 1404.

D.B. Miracle, O.N. Senkov, Acta Mater. 122 (2017) 448

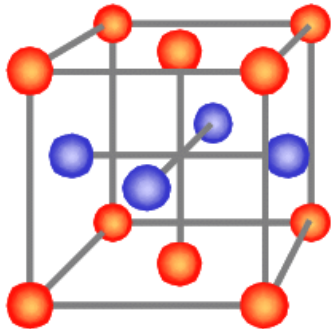
# Empirical parameters describing HEAs

- various atom sizes of elements → lattice distortions



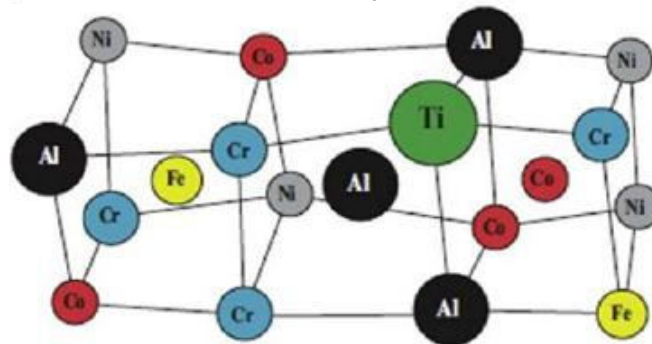
## conventional alloy

- constant lattice parameter
- constant crystalline structure



## high entropy alloy

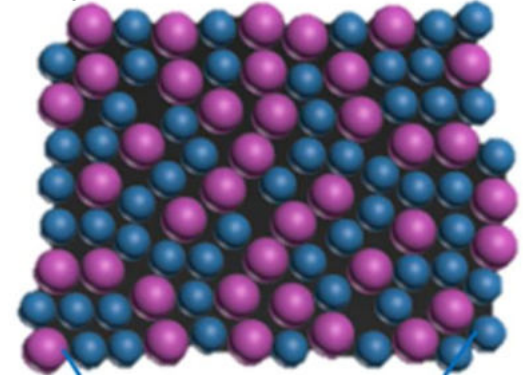
- lattice parameter varies
- constant crystalline structure



*lattice distortions*

## amorphous alloy

- lattice parameter varies
- crystalline structure varies



# Refractory metal HEAs

Group	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
Period 1	1 H																	2 He
Period 2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne
Period 3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
Period 4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
Period 5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
Period 6	55 Cs	56 Ba	57 La	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
Period 7	87 Fr	88 Ra	89 Ac	* 104 Rf	* 105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og
				* 58 Ce	* 59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu	
				* 90 Th	* 91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr	

refractory metals Hf, Nb, Ta, Ti, V, Zr



# Empirical parameters describing HEAs

- various atom sizes of elements → lattice distortions
- measure of lattice distortions – misfit parameter  $\delta$

**misfit parameter**

$$\delta = \sqrt{\sum_i c_i (1 - r_i/\bar{r})^2}$$

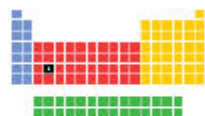
concentration  
of  $i$ -th element

atom radius  
of  $i$ -th element

composition  
weighted mean  
atom radius

# Atomic radius

$$\delta = \sqrt{\sum_i c_i (1 - r_i/\bar{r})^2}$$



[www.webelements.com](http://www.webelements.com)

72 Hf

Available hafnium properties...

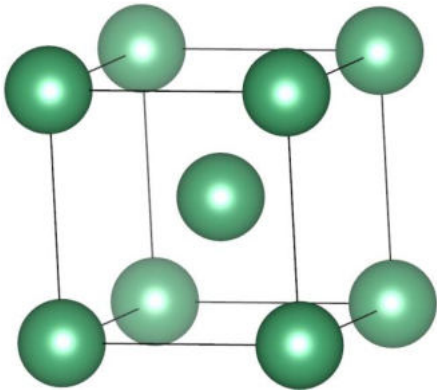
Essentials [More properties...](#)

Radius type	Radius value / pm	Periodicity link
<a href="#">Atomic radius (empirical)</a>	155	
<a href="#">Atomic radius (calculated)</a>	208	
<a href="#">Covalent radius (2008 values)</a>	175	
<a href="#">Molecular single bond covalent radius</a>	152 (coordination number 4)	
<a href="#">Molecular double bond covalent radius</a>	128	
<a href="#">Molecular triple bond covalent radius</a>	122	
<a href="#">Covalent radius (empirical)</a>	150	
<a href="#">van der Waals radius</a>	253	

# Atomic radius

- half of distance between elements in their equilibrium configuration

bcc structure



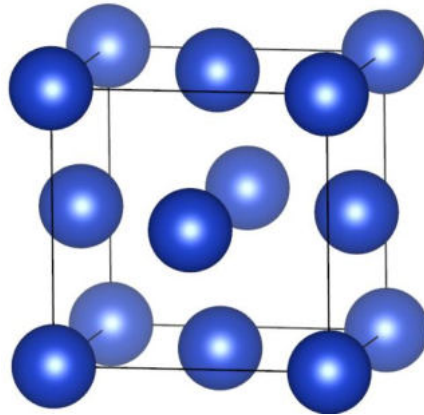
$$r = a \frac{\sqrt{3}}{4}$$

**Nb**,  $r = 1.44 \text{ \AA}$

**Ta**,  $r = 1.43 \text{ \AA}$

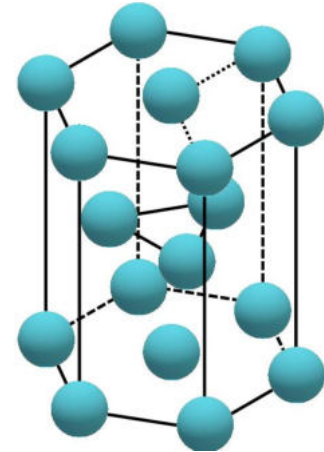
**V**,  $r = 1.31 \text{ \AA}$

fcc structure



$$r = a \frac{\sqrt{2}}{4}$$

hcp structure



$$r = \frac{1}{2} \sqrt{\frac{a^2}{3} + \frac{c^2}{4}}$$

**Hf**,  $r = 1.56 \text{ \AA}$

**Ti**,  $r = 1.45 \text{ \AA}$

**Zr**,  $r = 1.59 \text{ \AA}$

# Empirical parameters describing HEAs

- various atom sizes of elements → lattice distortions
- measure of lattice distortions – misfit parameter  $\delta$
- heat of solution  $H^{IM}$  vs. entropy  $S^{SS}$

$$-TS^{SS} \text{ vs. } H^{IM}$$

## misfit parameter

$$\delta = \sqrt{\sum_i c_i (1 - r_i/\bar{r})^2}$$

concentration  
of  $i$ -th element

atom radius  
of  $i$ -th element

composition  
weighted mean  
atom radius

## heat of solution of random SS

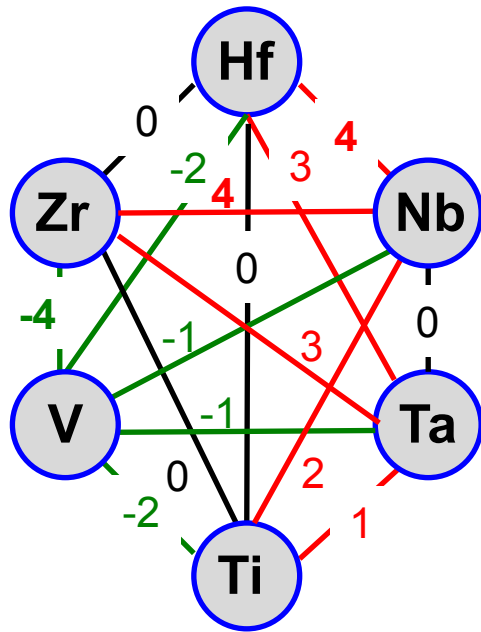
$$H^{SS} = \sum_{i < j} 4H_{i,j} c_i c_j$$

heat of solution for atomic pairs of  
elements  $i, j$  calculated using Miedena's  
model

A. Takeuchi, A. Inoue, Mater. Trans. 46 (2005) 2817

# Empirical parameters describing HEAs

- various atom sizes of elements → lattice distortions
- measure of lattice distortions – misfit parameter  $\delta$
- heat of solution  $H^{IM}$  vs. entropy  $S^{SS}$

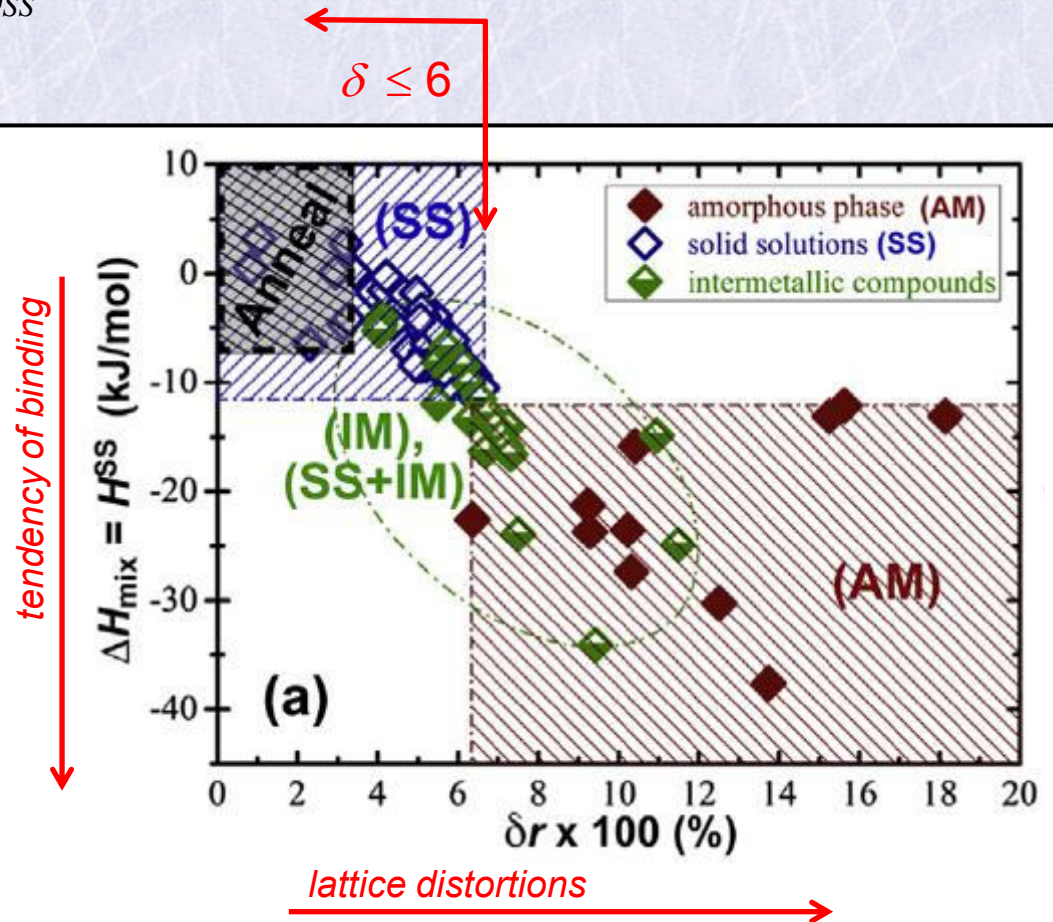
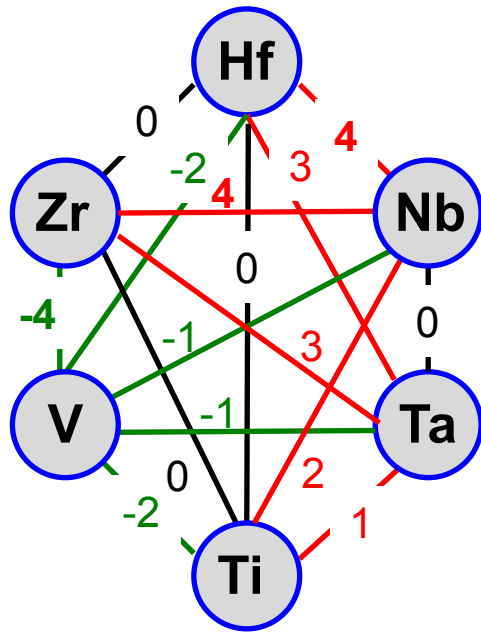


- repulsive interaction between (Nb,Ta) and (Zr,Hf)

binary heat of solutions  $H_{i,j}$

# Empirical parameters describing HEAs

- various atom sizes of elements → lattice distortions
- measure of lattice distortions – misfit parameter  $\delta$
- heat of solution  $H^{IM}$  vs. entropy  $S^{SS}$



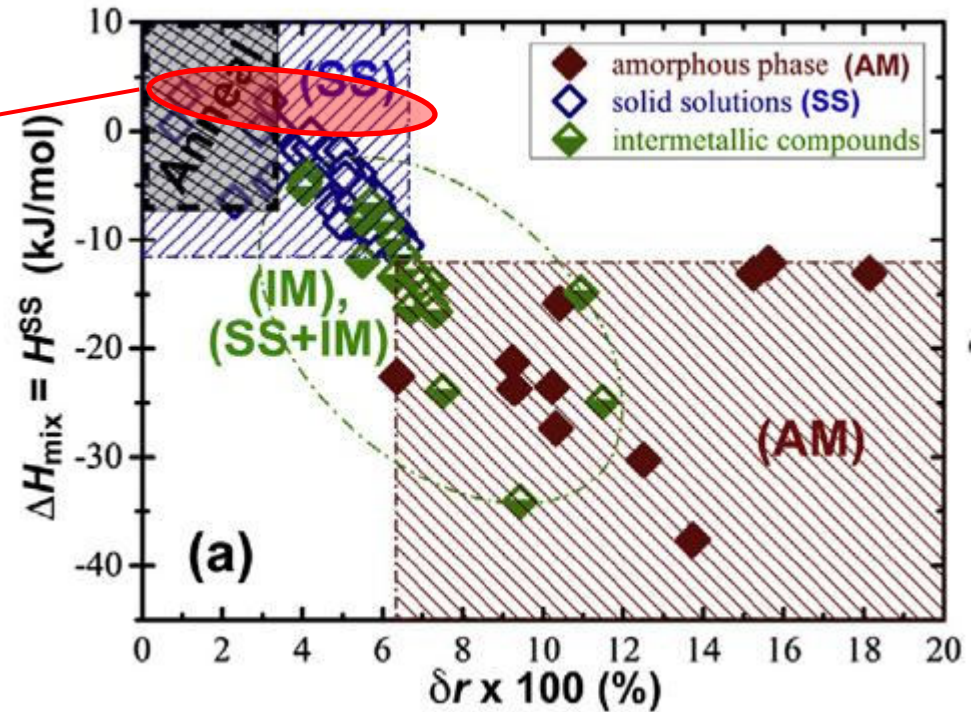
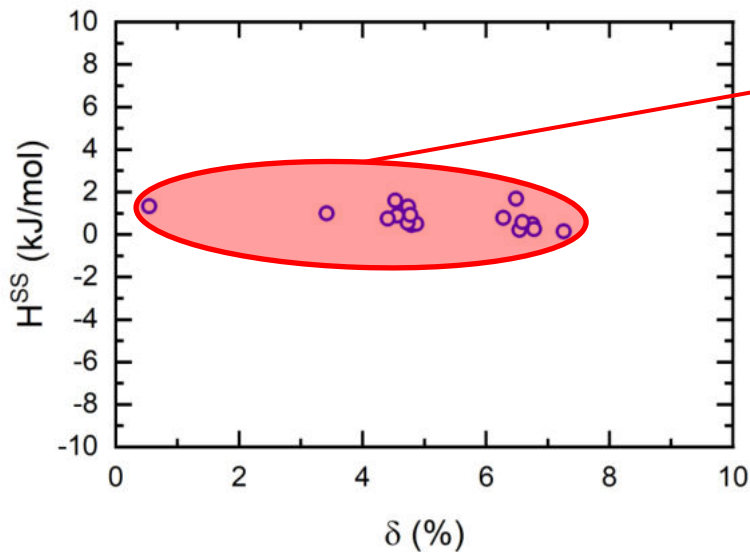
# Alloys studied

- 17 alloys
- concentrated solutions of refractory metals  
Hf, Nb, Ta, Ti, V, Zr
- all alloys have bcc structure

Alloy	$S^{SS}(R)$	$\delta$ (%)	$H^{SS}$ (kJ/mol)
NbTaTi	1.10	1.05	1.33
NbTiZr	1.10	5.03	0.89
TaTiZr	1.10	5.01	0.44
NbTaTiZr	1.39	4.83	0.75
NbTiVZr	1.39	7.04	0.25
Nb <sub>0.5</sub> TaTiZr <sub>1.5</sub>	1.32	5.22	0.50
Nb <sub>1.5</sub> TaTiZr <sub>0.5</sub>	1.32	3.83	1.00
Nb <sub>2</sub> TaTiZr <sub>2</sub>	1.33	5.27	0.56
Nb <sub>2</sub> TiVZr <sub>2</sub>	1.33	6.91	0.22
HfNb <sub>4</sub> TaTiZr <sub>4</sub>	1.39	5.43	0.93
HfNbTaTiZr	1.61	4.98	1.60
HfNbTiVZr	1.61	7.06	0.48
Hf <sub>0.5</sub> Nb <sub>1.5</sub> TiV <sub>1.5</sub> Zr <sub>0.5</sub>	1.50	6.70	1.68
Hf <sub>0.75</sub> Nb <sub>0.75</sub> TiV <sub>1.25</sub> Zr <sub>1.25</sub>	1.58	7.53	0.15
HfNbTiVZr <sub>0.5</sub>	1.58	6.88	0.59
Hf <sub>0.5</sub> NbTa <sub>0.5</sub> TiZr	1.56	5.00	1.31
HfNbTaTiVZr	1.79	6.58	0.78

# Empirical parameters describing HEAs

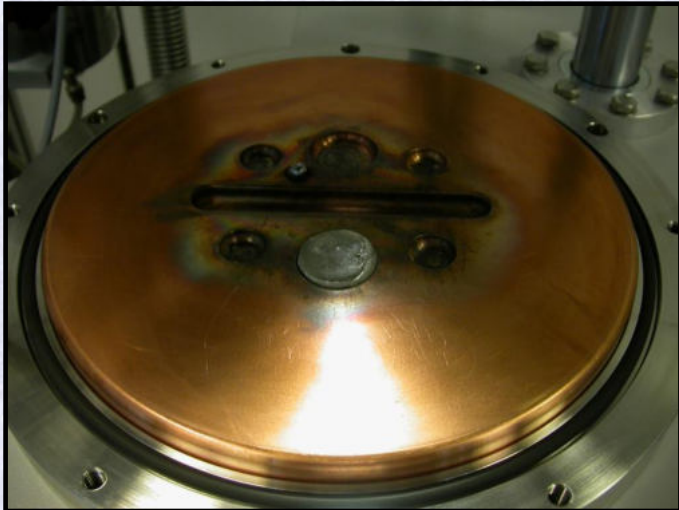
- various atom sizes of elements → lattice distortions
- measure of lattice distortions – misfit parameter  $\delta$
- heat of solution  $H^{IM}$  vs. entropy  $S^{SS}$





# Preparation of samples

- casting from 99.99% elements
- UHV arc melting (base pressure  $5 \times 10^{-6}$  mbar)
- Edmund Bühler AM200, max. temperature 3500°C
- water cooled Cu plate mould
- ingot diameter 30 mm



# Preparation of samples

- $10 \times 10 \times 1 \text{ mm}^3$  samples for positron annihilation studies were cut from ingots using diamond saw



# Preparation of samples

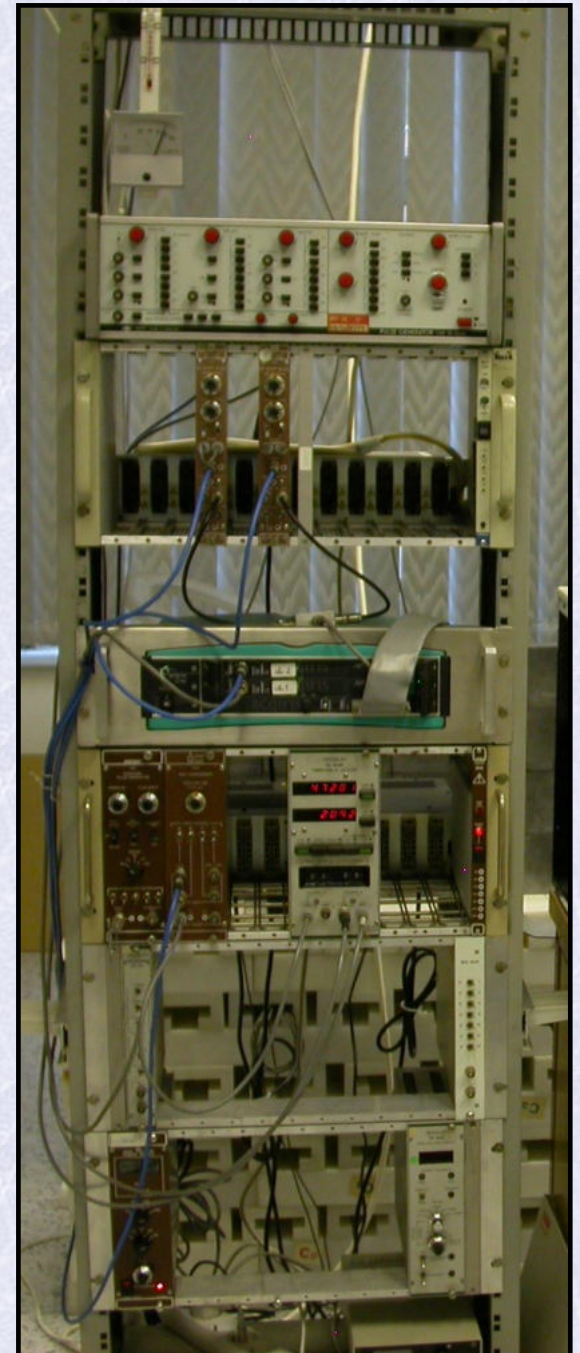
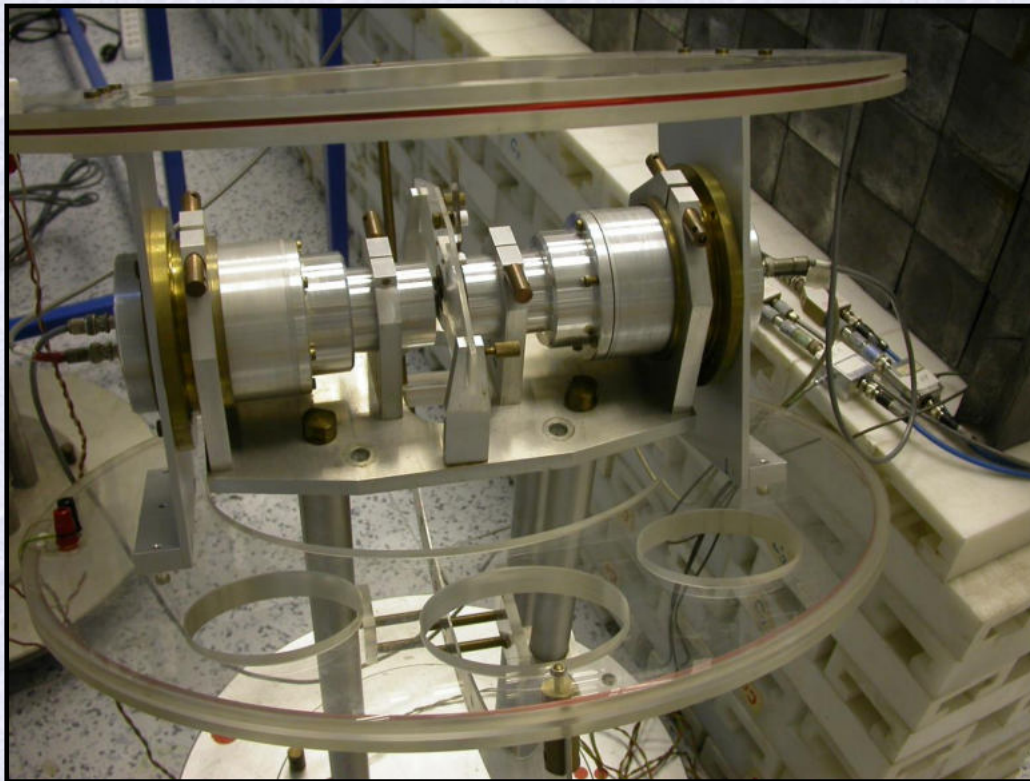
- $10 \times 10 \times 1 \text{ mm}^3$  samples for positron annihilation studies were cut from ingots using diamond saw
- samples were annealed in UHV ( $10^{-6}$  mbar) at  $1200^\circ\text{C}$  for 2 h
- annealing was finished by quenching



# Positron lifetime investigations

- digital positron lifetime spectrometer
- photomultipliers Hamamatsu H3378
- BaF<sub>2</sub> scintillators
- time resolution 145 ps (FWHM <sup>22</sup>Na)
- effective coincidence count rate 100 s<sup>-1</sup>
- >10<sup>7</sup> positron annihilation events in each spectrum

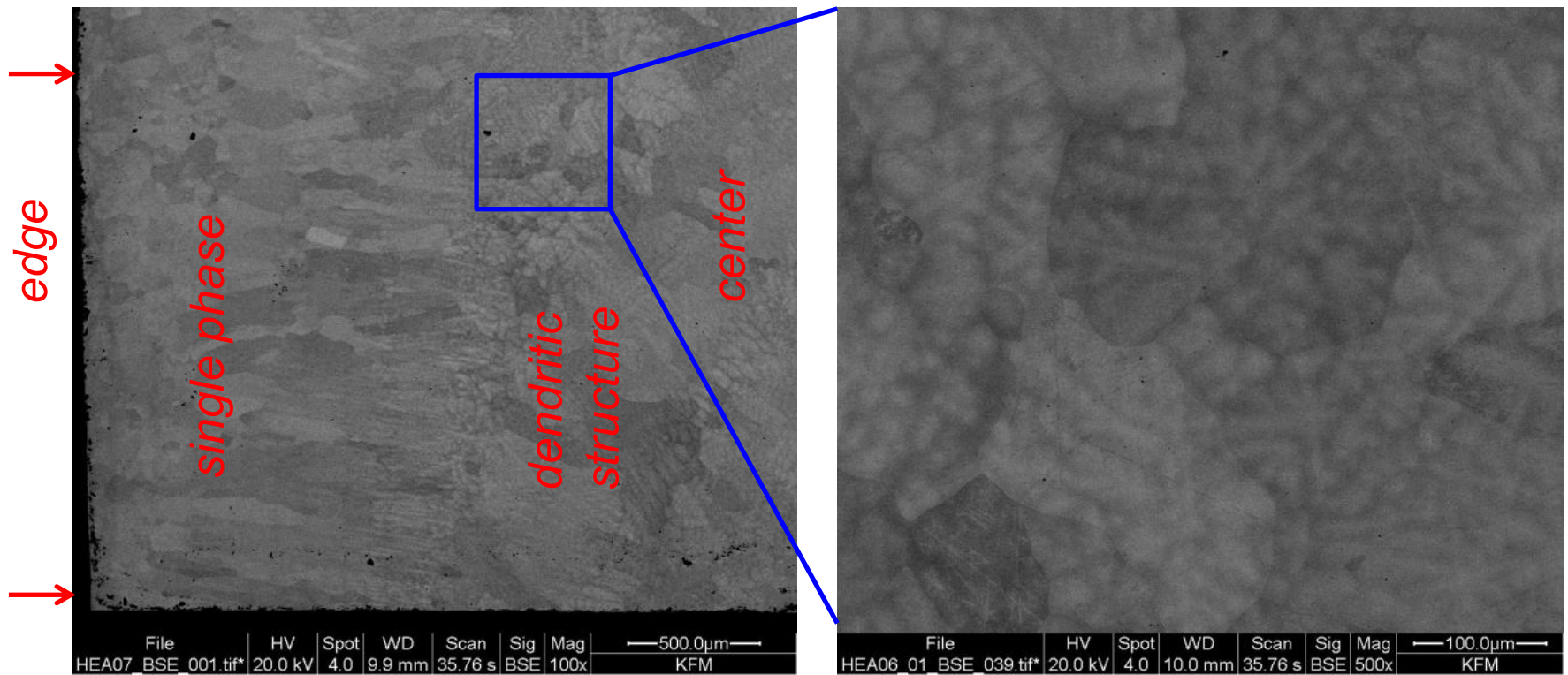
*F. Bečvář et al., Nucl. Instrum. Methods A 539, 372 (2005)*



# HfNbTaTiZr alloy - microstructure

- as-cast state

- scanning electron microscopy (back-scattered electrons)



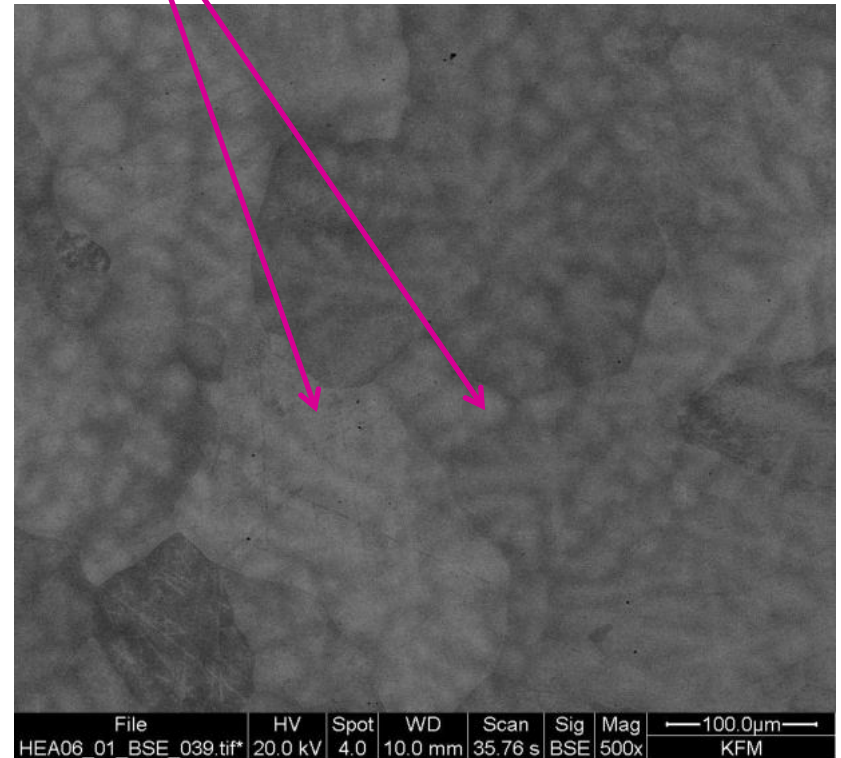
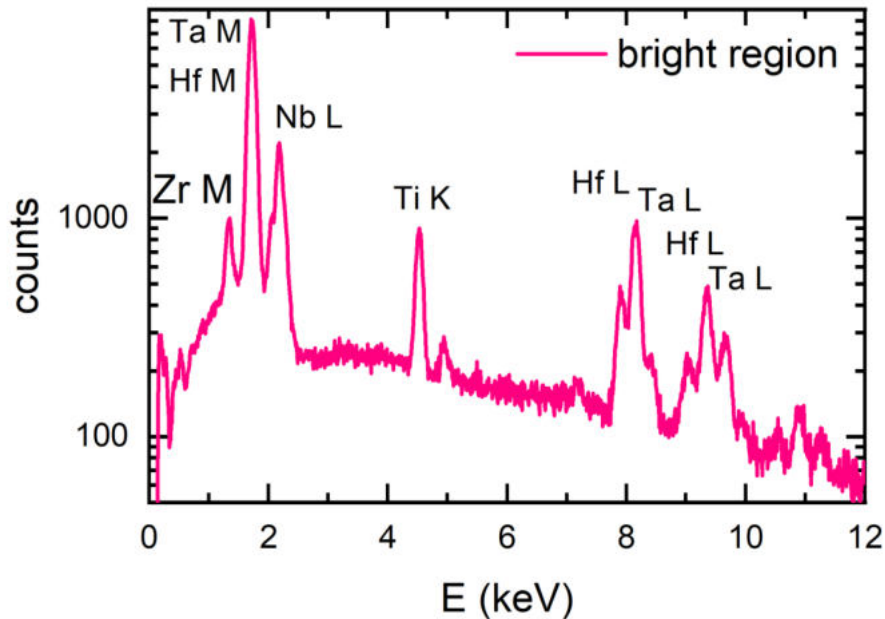
# HfNbTaTiZr alloy - microstructure

- as-cast state

scanning electron microscopy (back-scattered electrons)

bright regions  
enriched in Nb,Ta

energy dispersive X-ray spectroscopy (EDS)



# HfNbTaTiZr alloy - microstructure

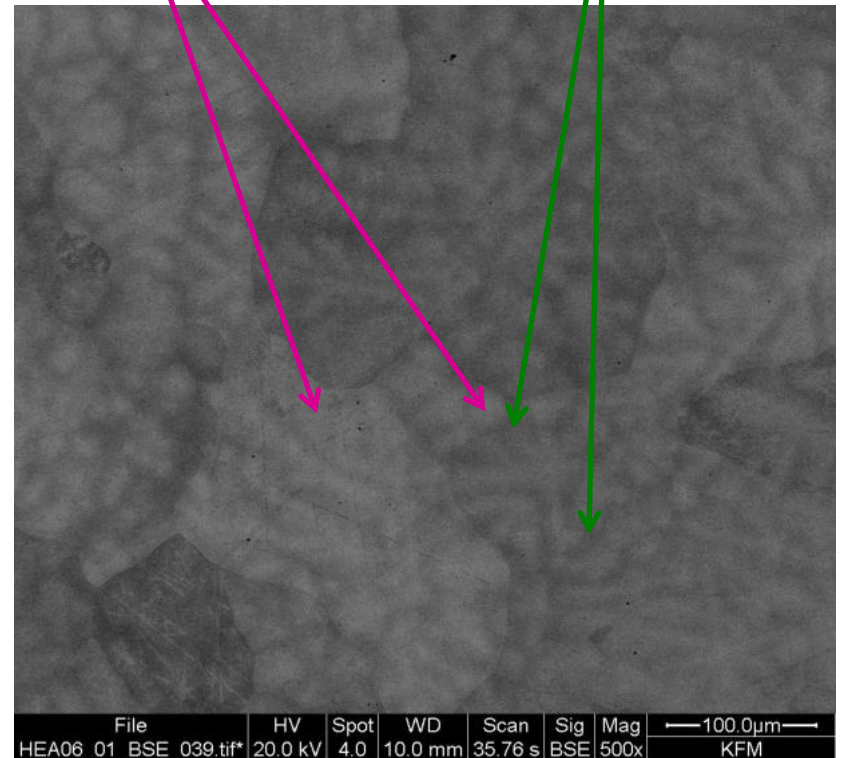
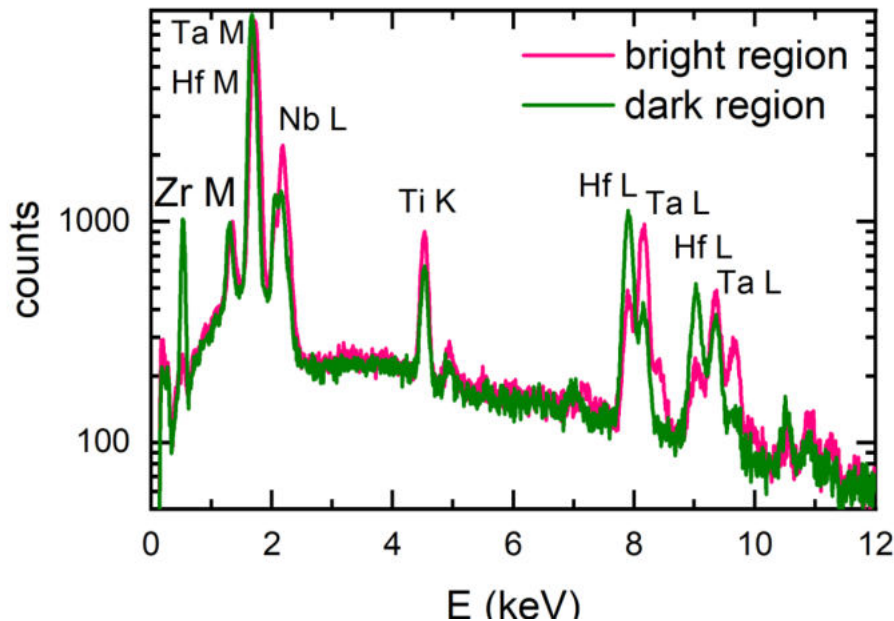
- as-cast state

scanning electron microscopy (back-scattered electrons)

bright regions  
enriched in Nb,Ta

dark regions  
enriched in Hf,Zr

energy dispersive X-ray spectroscopy (EDS)



# HfNbTaTiZr alloy - microstructure

- as-cast state

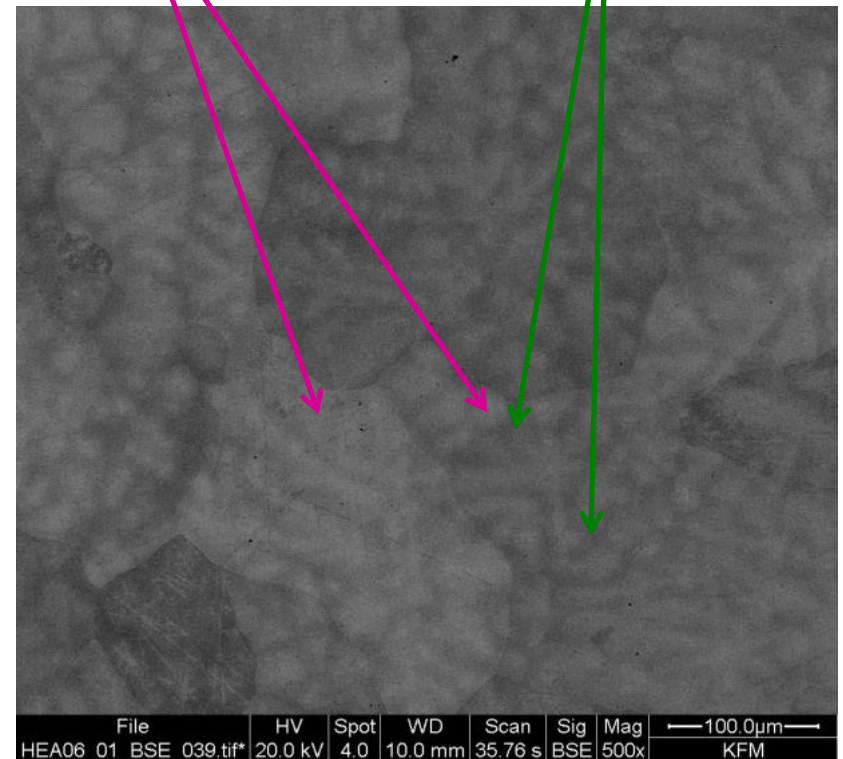
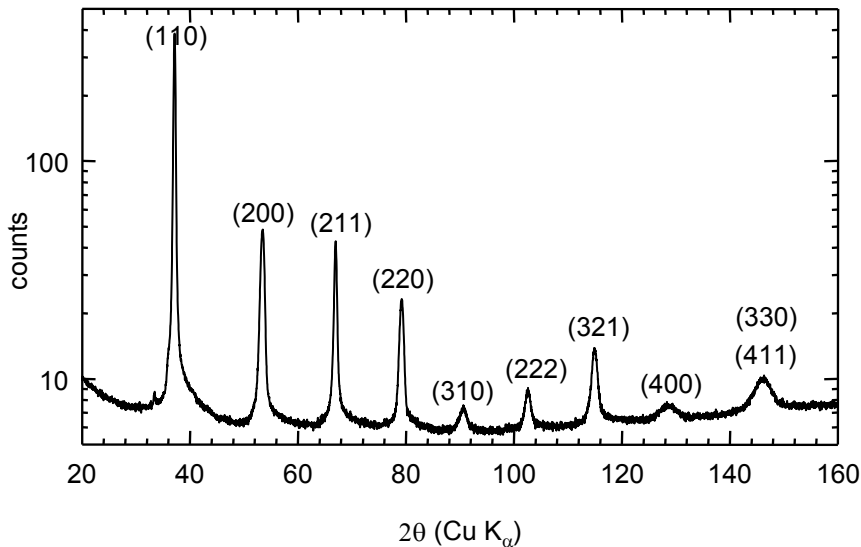
scanning electron microscopy (back-scattered electrons)

bright regions  
enriched in Nb,Ta

dark regions  
enriched in Hf,Zr

X-ray diffraction

- bcc structure,  $a = 3.404 \text{ \AA}$



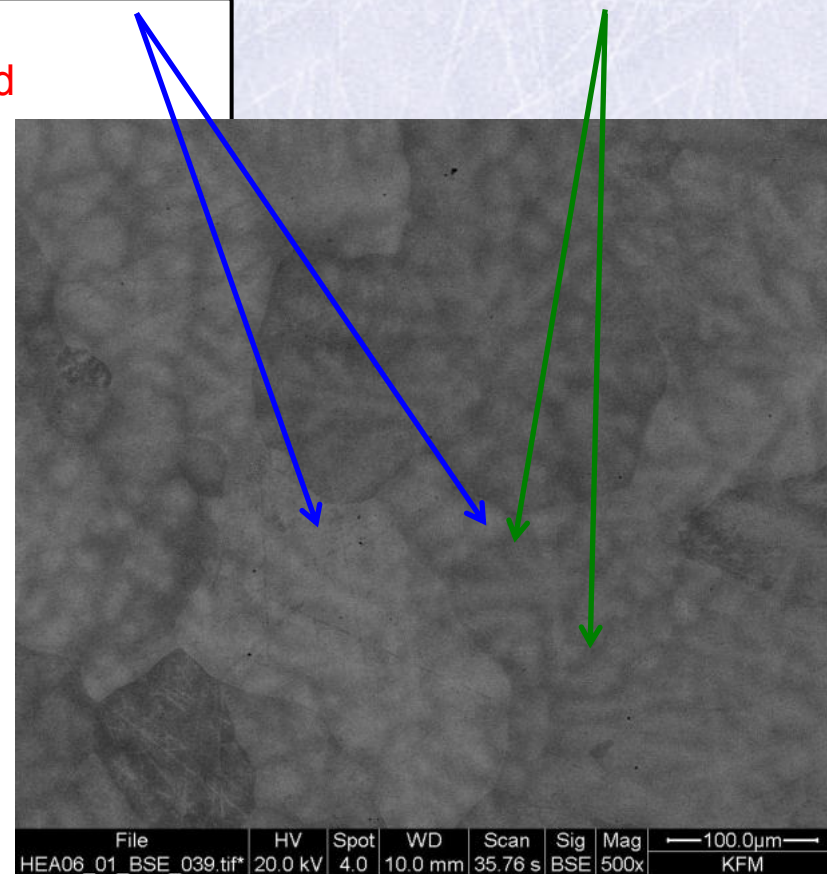
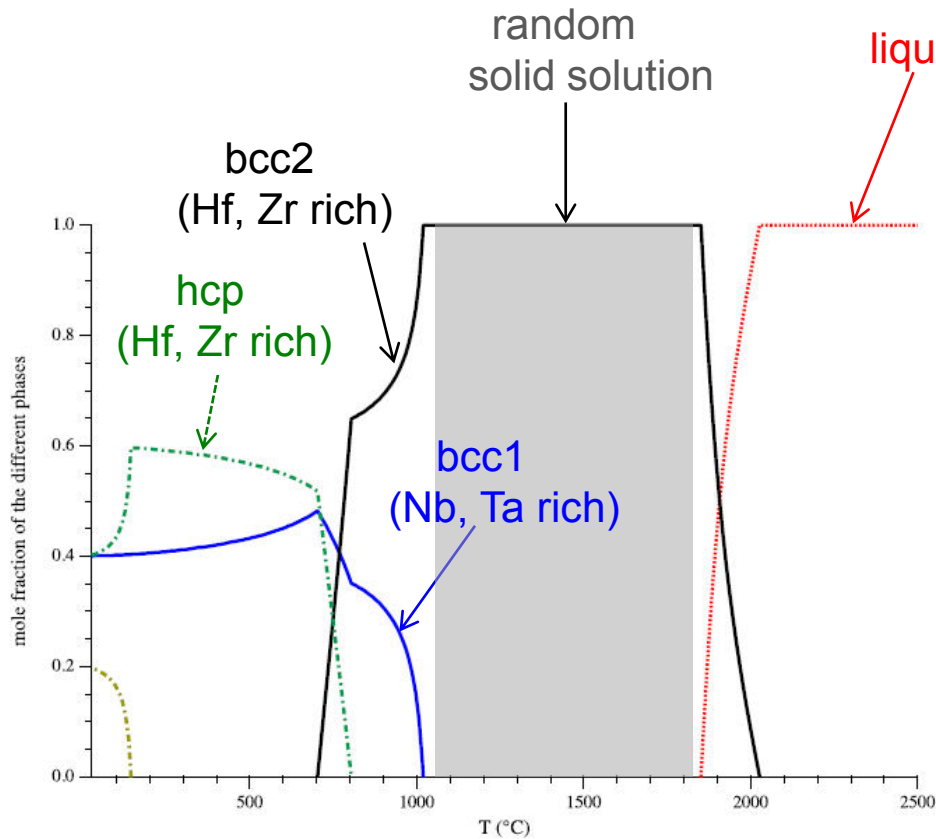


# HfNbTaTiZr alloy - microstructure

- Calphad modelling

**bcc1**  
bright regions  
enriched in Nb,Ta

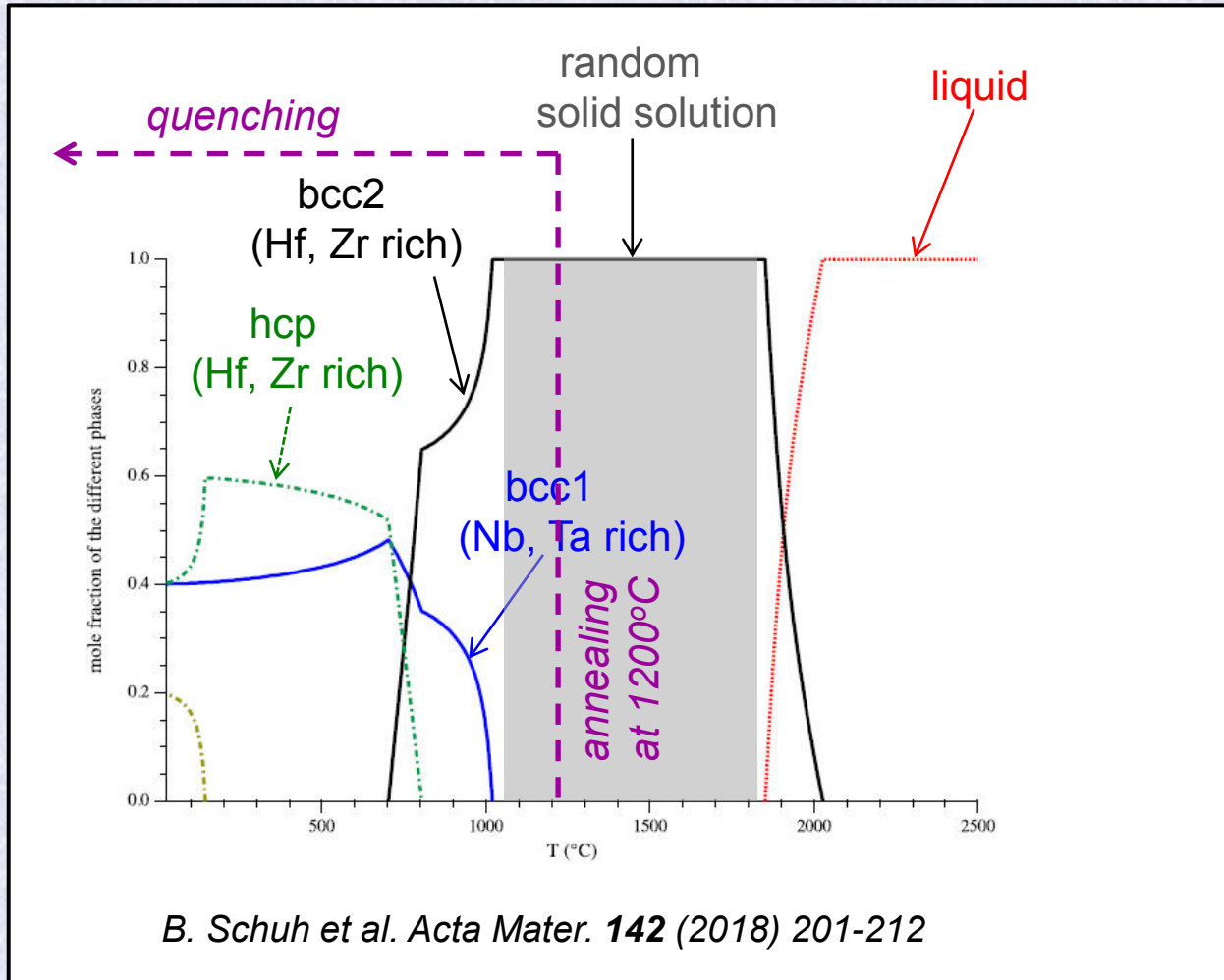
**bcc2**  
dark regions  
enriched in Hf,Zr



B. Schuh et al. *Acta Mater.* **142** (2018) 201-212

# HfNbTaTiZr alloy - microstructure

- Calphad modelling

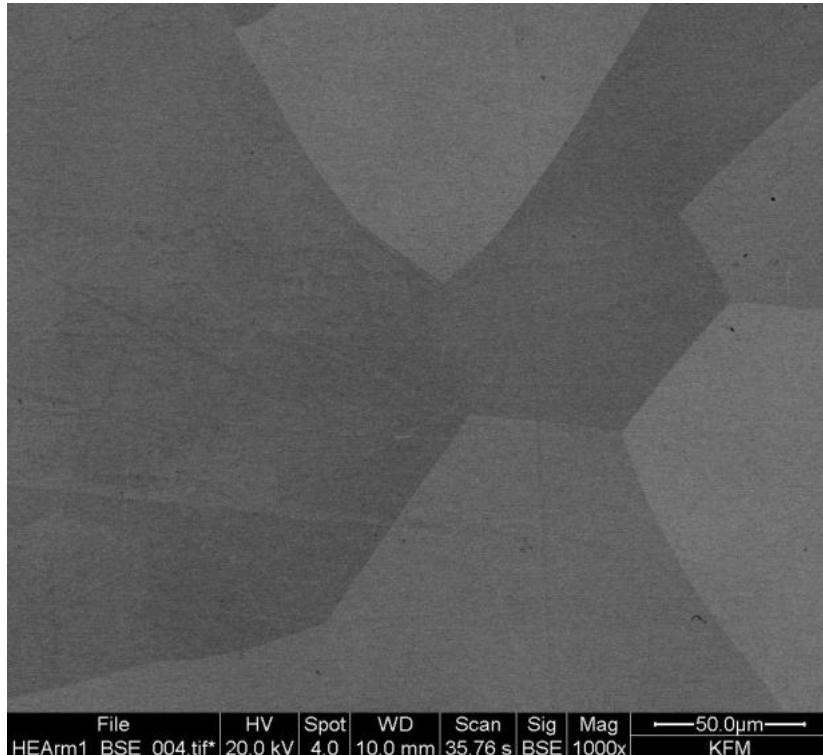


# HfNbTaTiZr alloy - microstructure

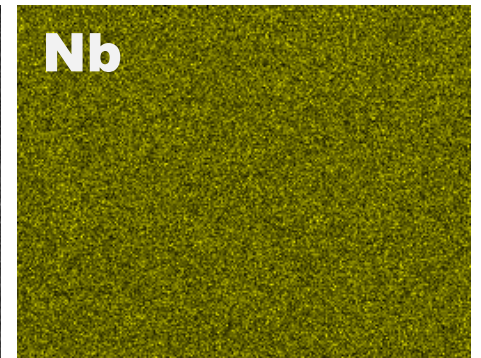
sample annealed in vacuum at 1200°C/2h

EDS elemental mapping

scanning electron microscopy  
(back-scattered electrons)



SE



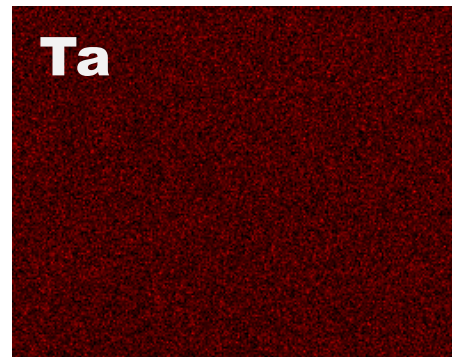
Nb



Ti



Hf



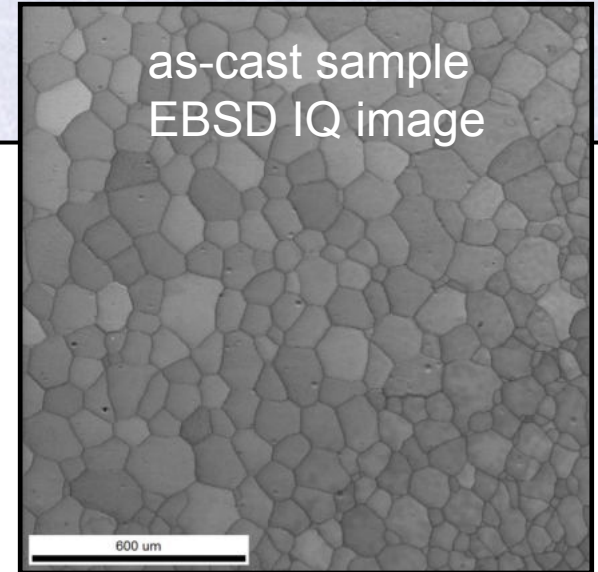
Ta



Zr

# HfNbTaTiZr alloy – positron lifetime spectroscopy

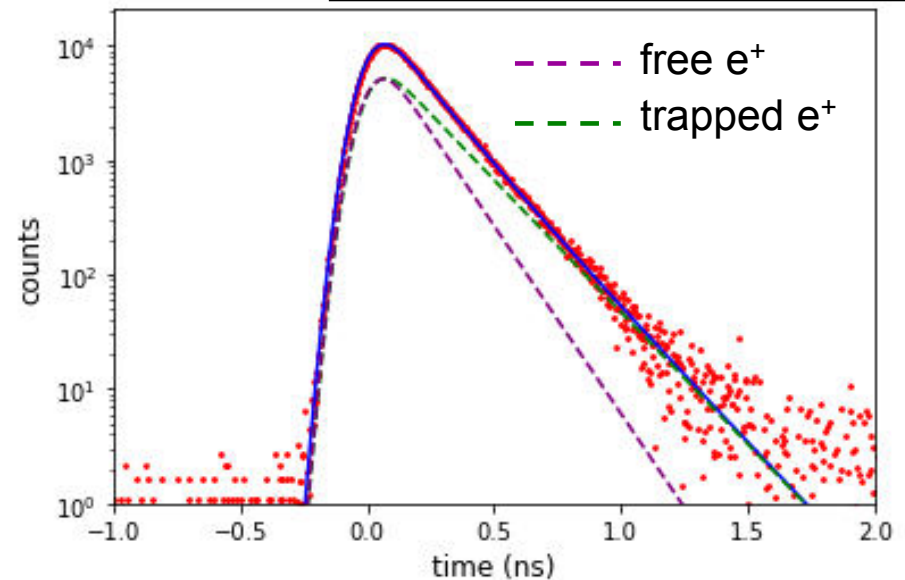
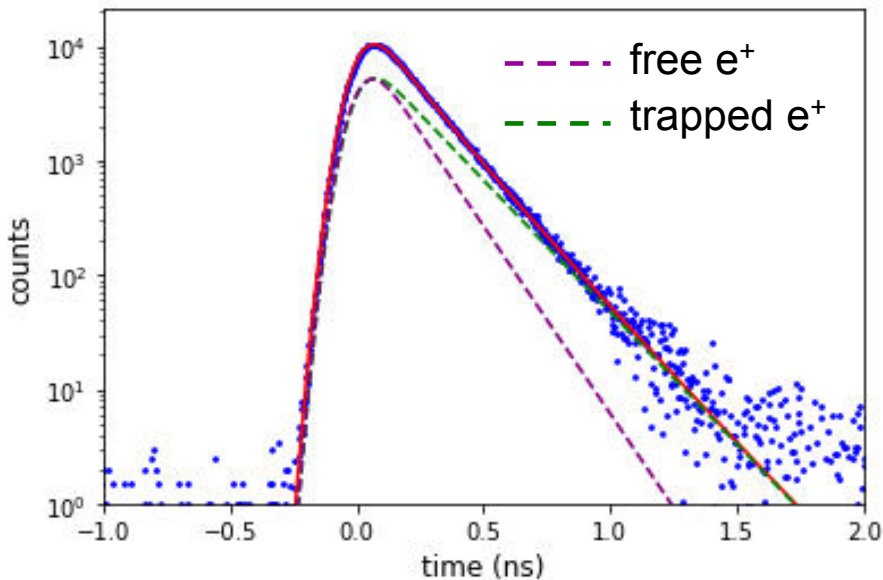
- as-cast state



state	$\tau_1$ (ps)	$I_1$ (%)	$\tau_2$ (ps)	$I_2$ (%)
as-cast	105(7)	31(3)	189(2)	69(3)

free positrons

positrons trapped at dislocations



positron lifetime spectrum with subtracted source contribution

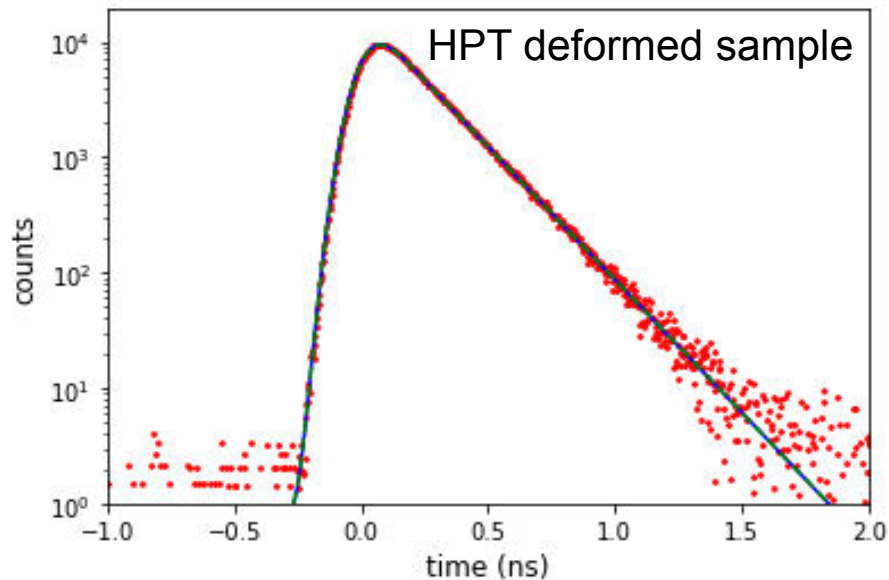
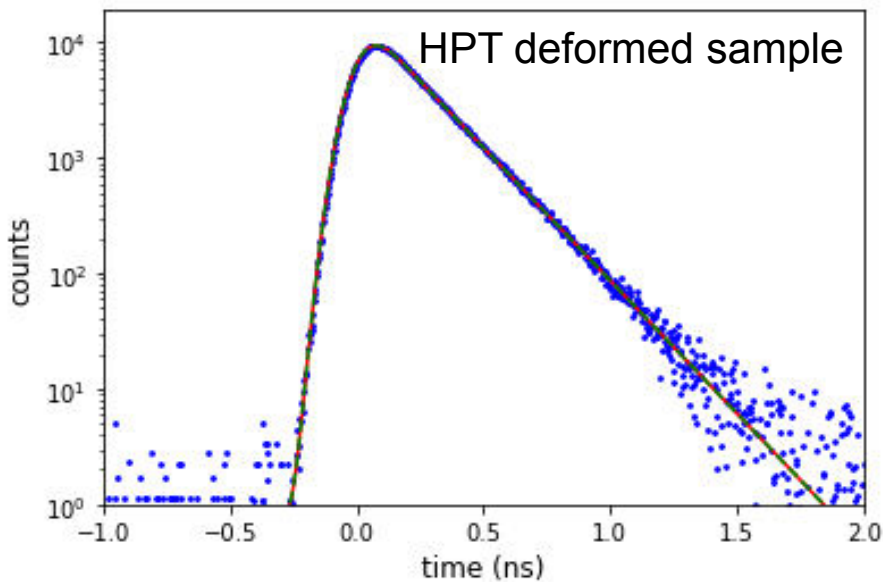
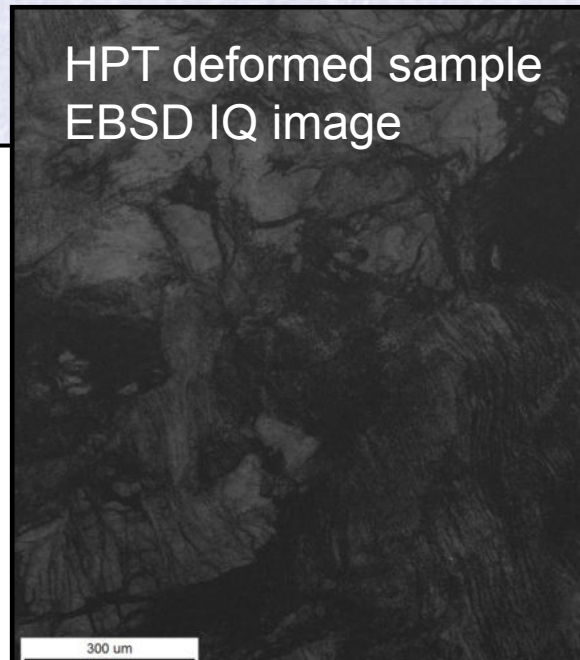
# HfNbTaTiZr alloy – positron lifetime spectroscopy

- deformed samples:  
cold rolling, high pressure torsion (HPT)

HPT deformed sample  
EBSD IQ image

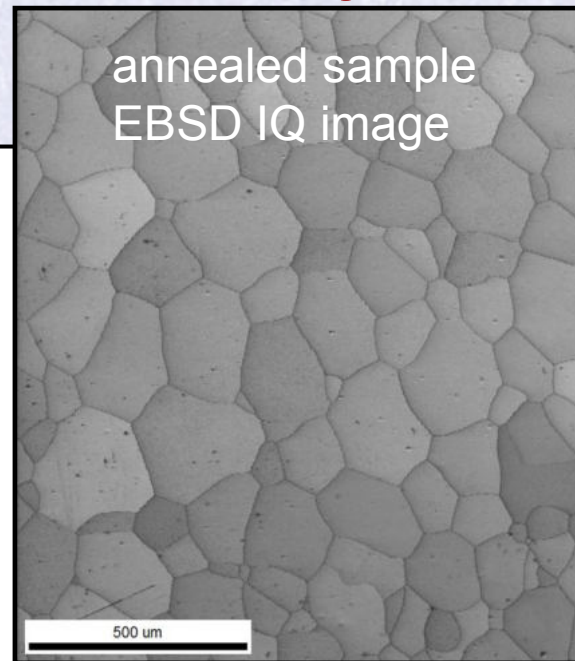
free positrons  
positrons trapped at dislocations

state	$\tau_1$ (ps)	$I_1$ (%)	$\tau_2$ (ps)	$I_2$ (%)
as-cast	105(7)	31(3)	189(2)	69(3)
cold rolled	58(4)	12(2)	186(2)	88(2)
HPT deformed	-	-	188(1)	100



# HfNbTaTiZr alloy – positron lifetime spectroscopy

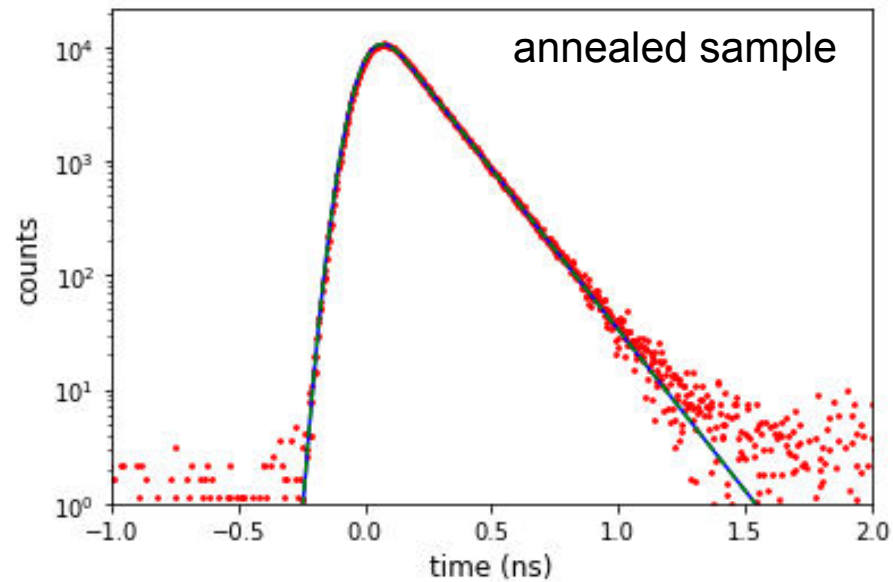
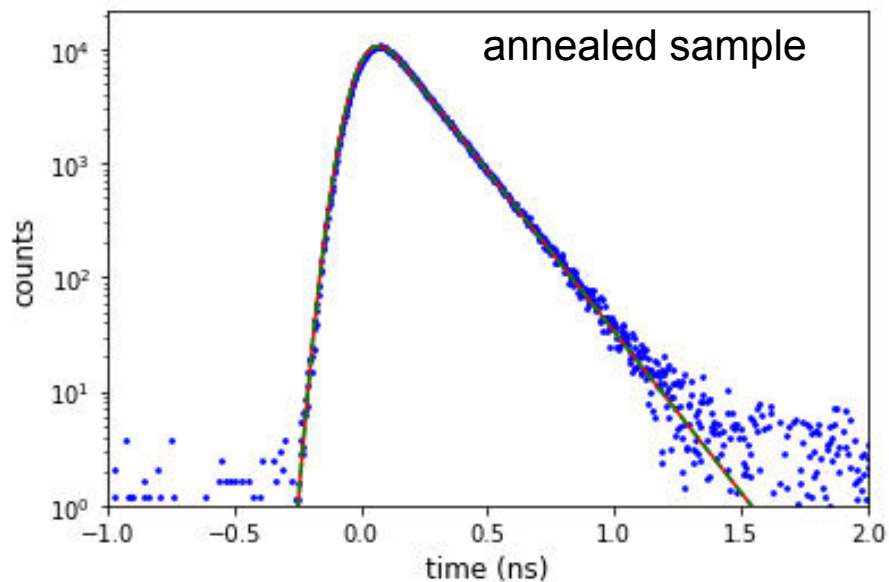
- sample annealed in vacuum at 1200°C for 1h



free positrons

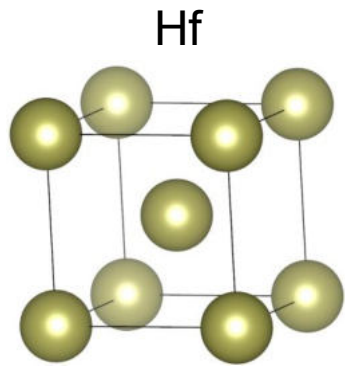


state	$\tau_1$ (ps)	$I_1$ (%)	$\tau_2$ (ps)	$I_2$ (%)
annealed	141(1)	100	-	-

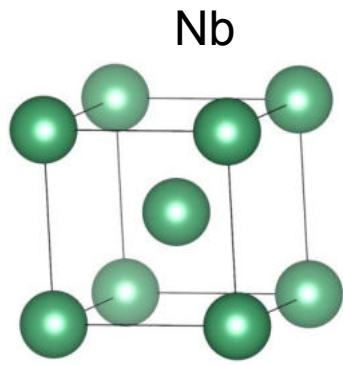


# HfNbTaTiZr – positron lifetime calculations

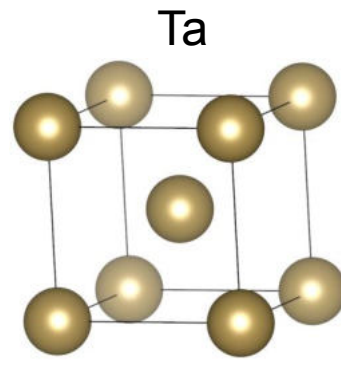
- bcc structure  $a = 3.4 \text{ \AA}$



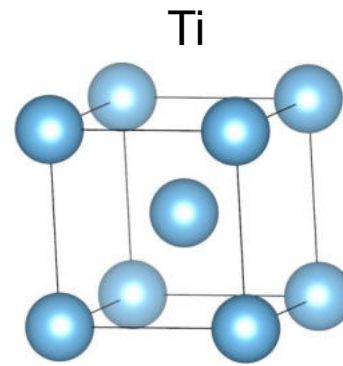
$$\tau = 132 \text{ ps}$$



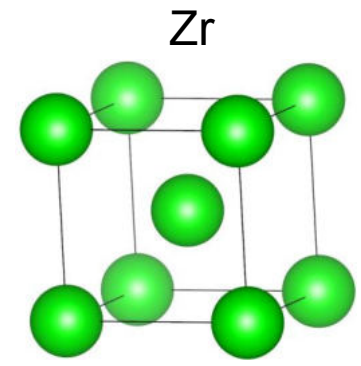
$$\tau = 138 \text{ ps}$$



$$\tau = 130 \text{ ps}$$



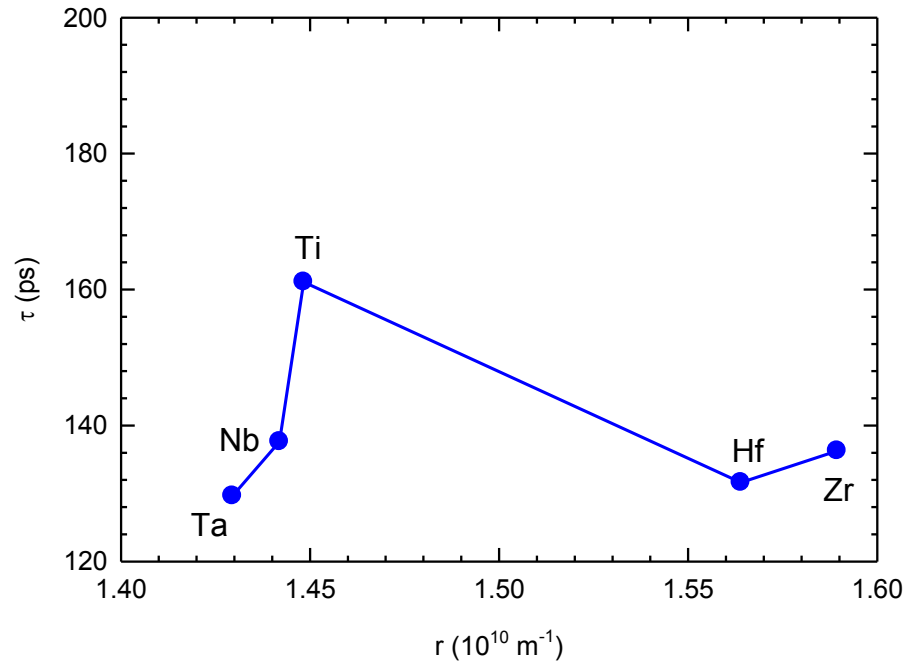
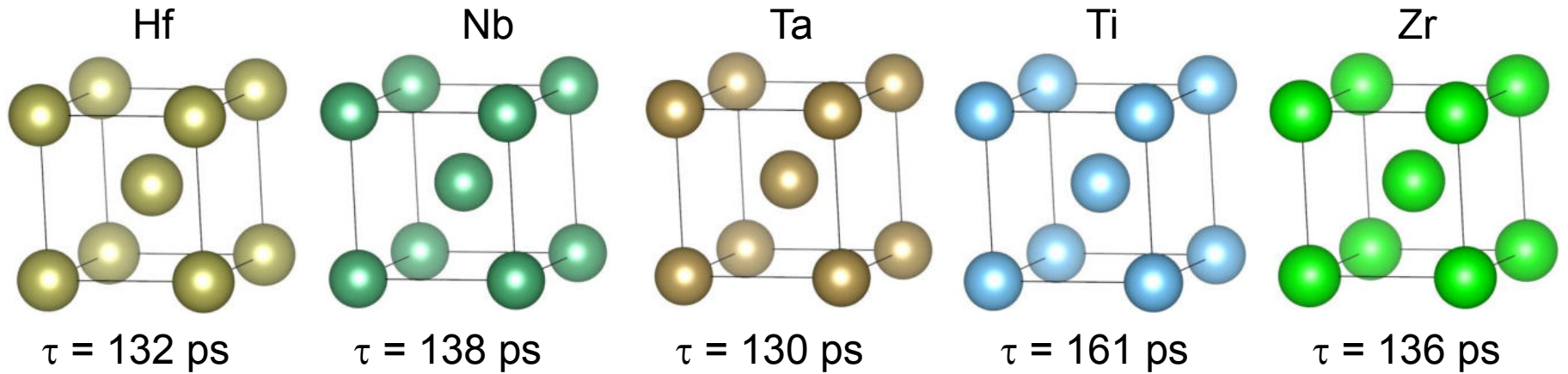
$$\tau = 161 \text{ ps}$$



$$\tau = 136 \text{ ps}$$

# HfNbTaTiZr – positron lifetime calculations

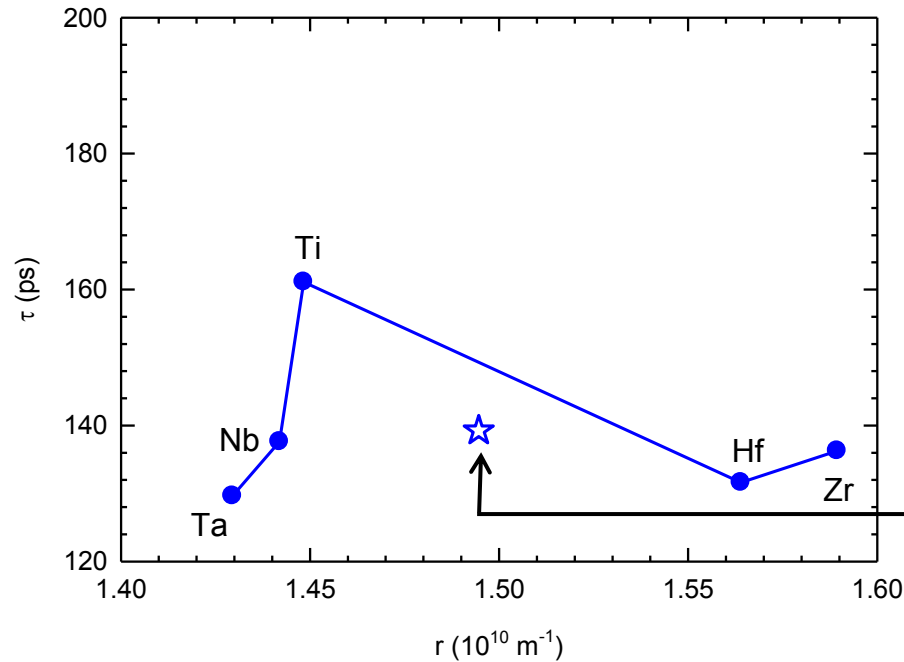
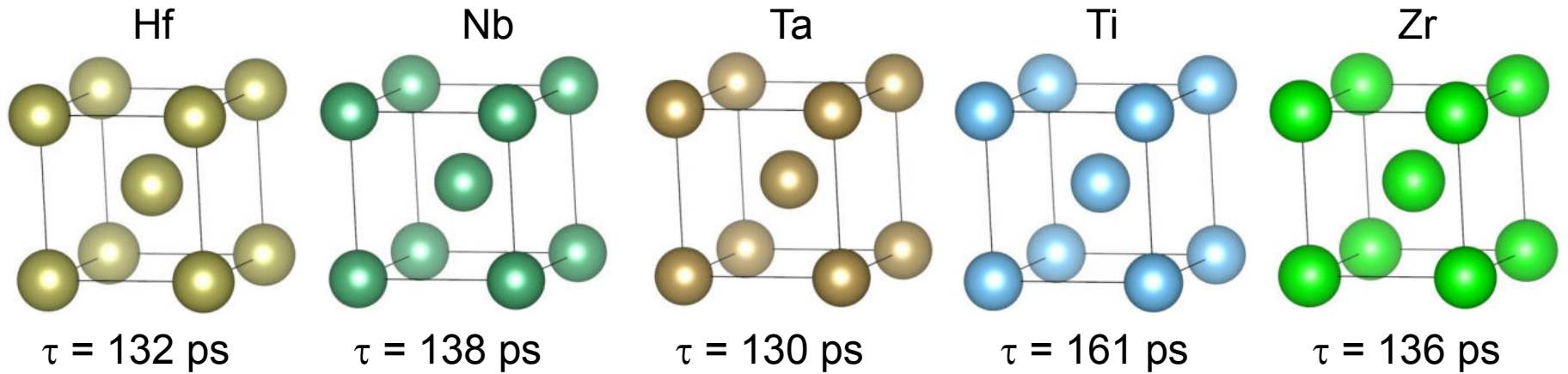
- bcc structure  $a = 3.4 \text{ \AA}$





# HfNbTaTiZr – positron lifetime calculations

- bcc structure  $a = 3.4 \text{ \AA}$

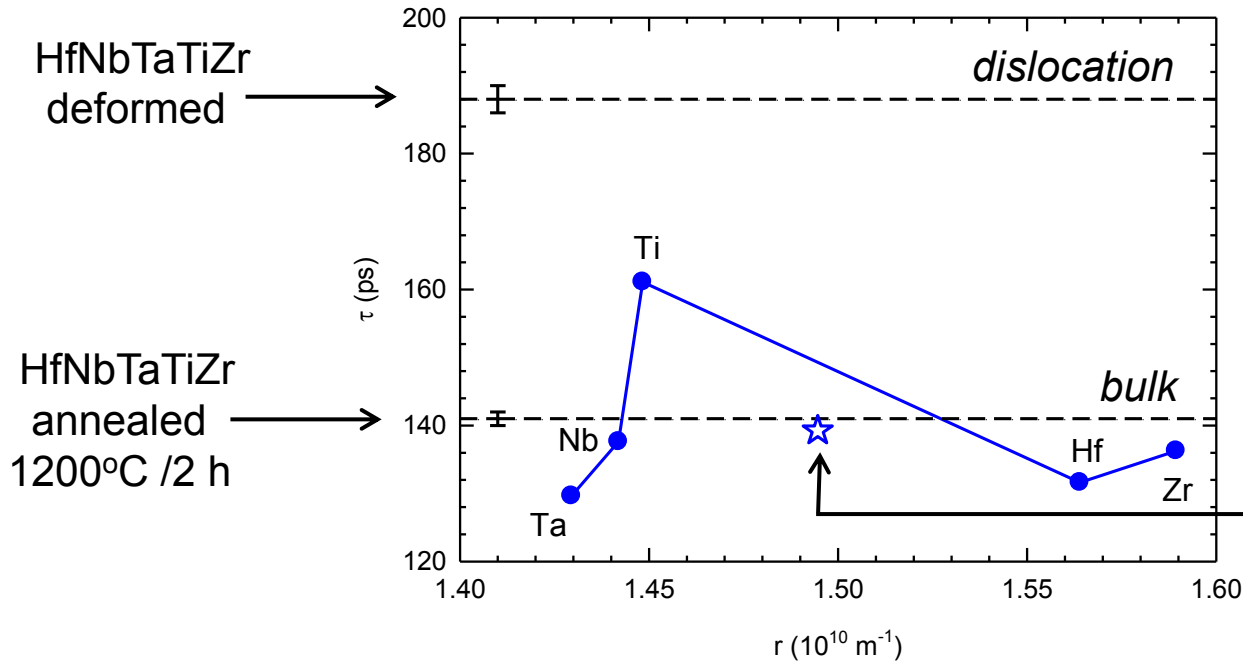
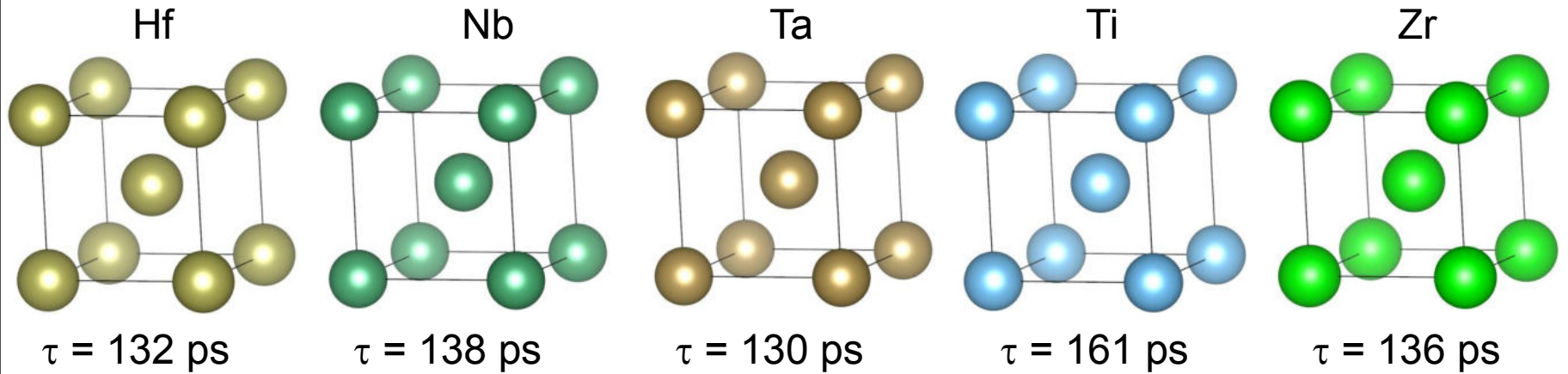


weighted average

$$\bar{\tau}_w = \sum_i C_i \tau_i$$

# HfNbTaTiZr – positron lifetime calculations

- bcc structure  $a = 3.4 \text{ \AA}$

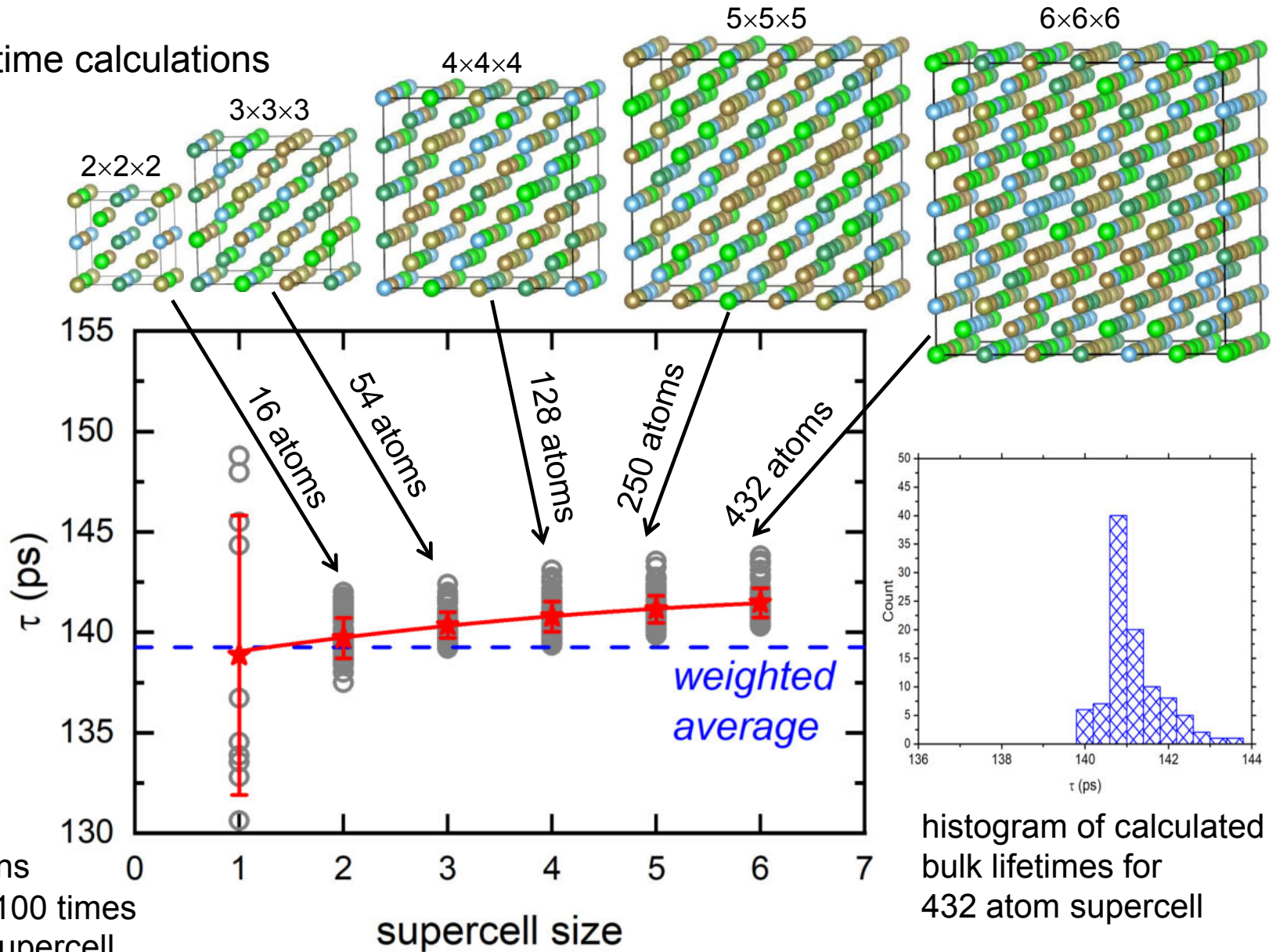


weighted average

$$\bar{\tau}_w = \sum_i C_i \tau_i$$

# HfNbTaTiZr – positron lifetime calculations

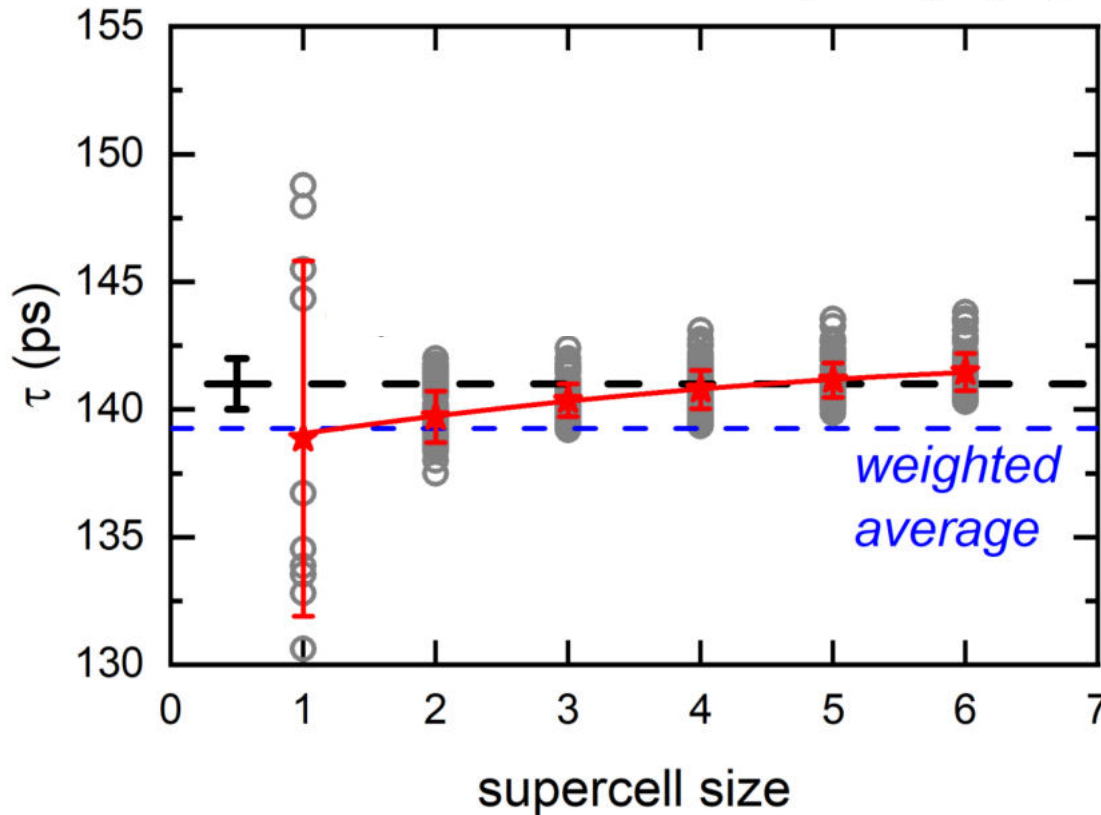
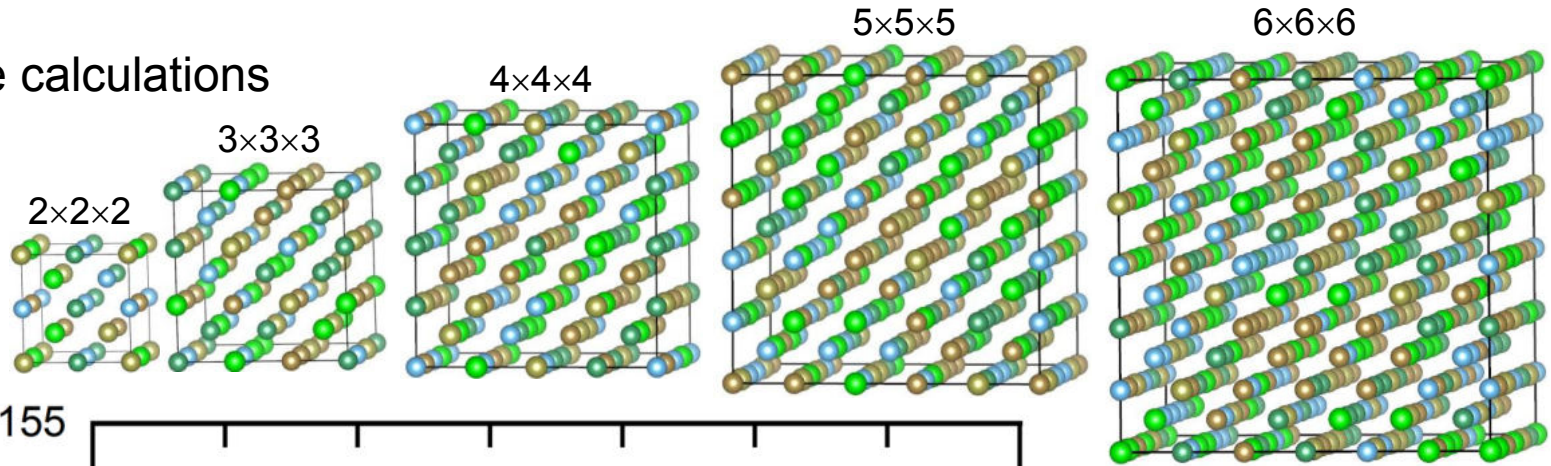
- bulk lifetime calculations



- calculations repeated 100 times for each supercell

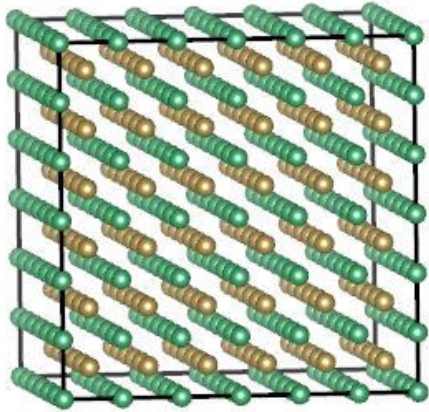
# HfNbTaTiZr – positron lifetime calculations

- bulk lifetime calculations



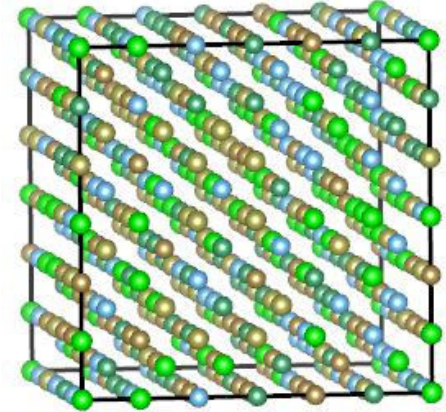
# HfNbTaTiZr – positron lifetime calculations

ordered alloy (NbTa)

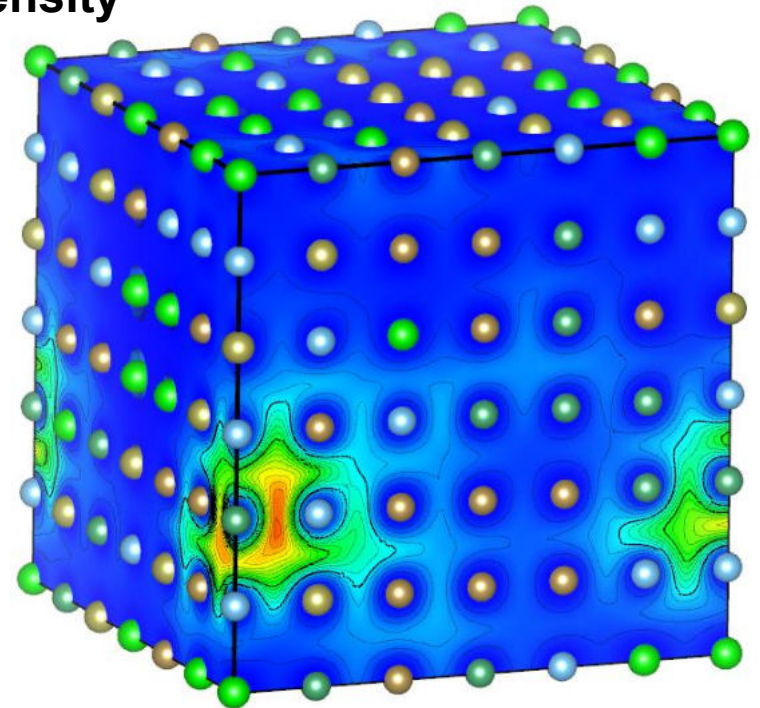
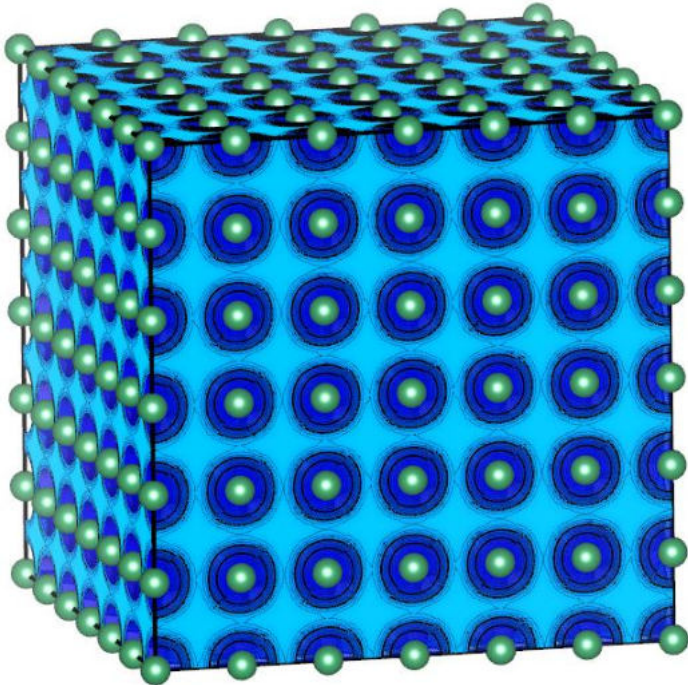


- $e^+$  searches for interstitial regions with enhanced open volume
- $e^+$  can be used as a probe of lattice distortions
- one can expect positive correlation between bulk  $e^+$  lifetime and magnitude of lattice distortions

HEA (HfNbTaTiZr)

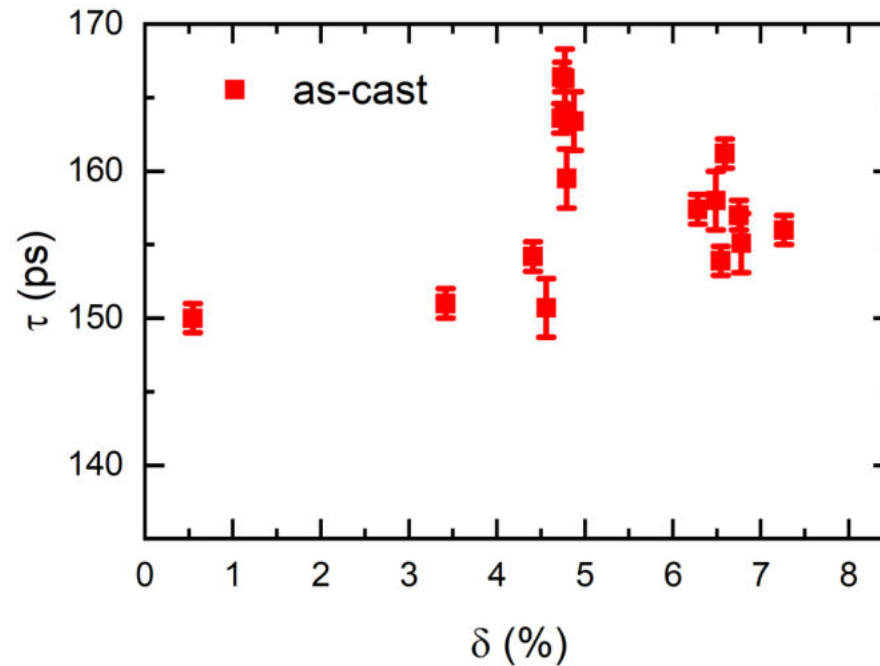


calculated positron density



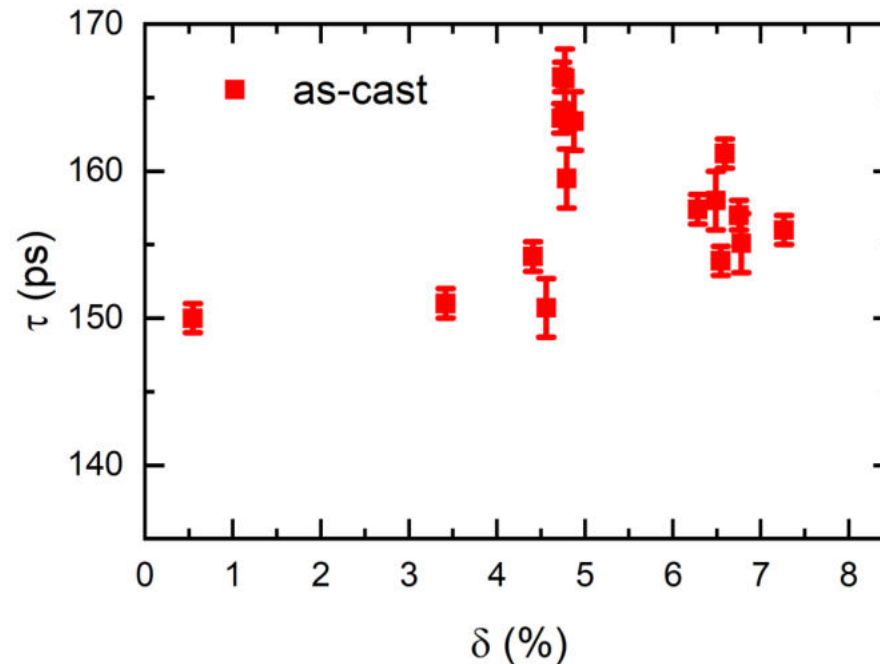
# Positron lifetime investigations of HEAs

- mean positron lifetime  $\rightarrow$  single component fit of positron lifetime spectra
- as-cast alloys



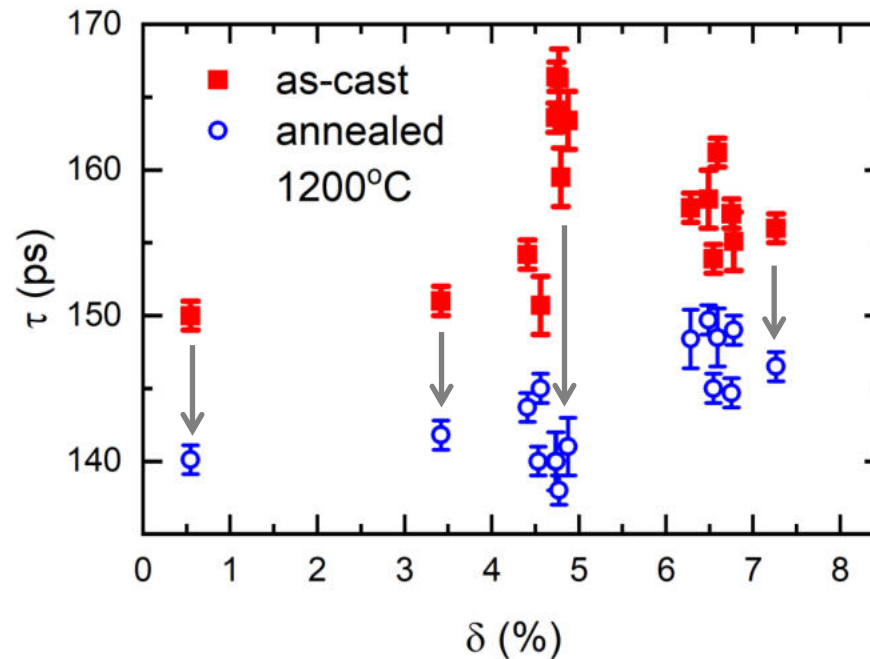
# Positron lifetime investigations of HEAs

- mean positron lifetime  $\rightarrow$  single component fit of positron lifetime spectra
- as-cast alloys  $\rightarrow$  significant contribution of positrons trapped at dislocations



# Positron lifetime investigations of HEAs

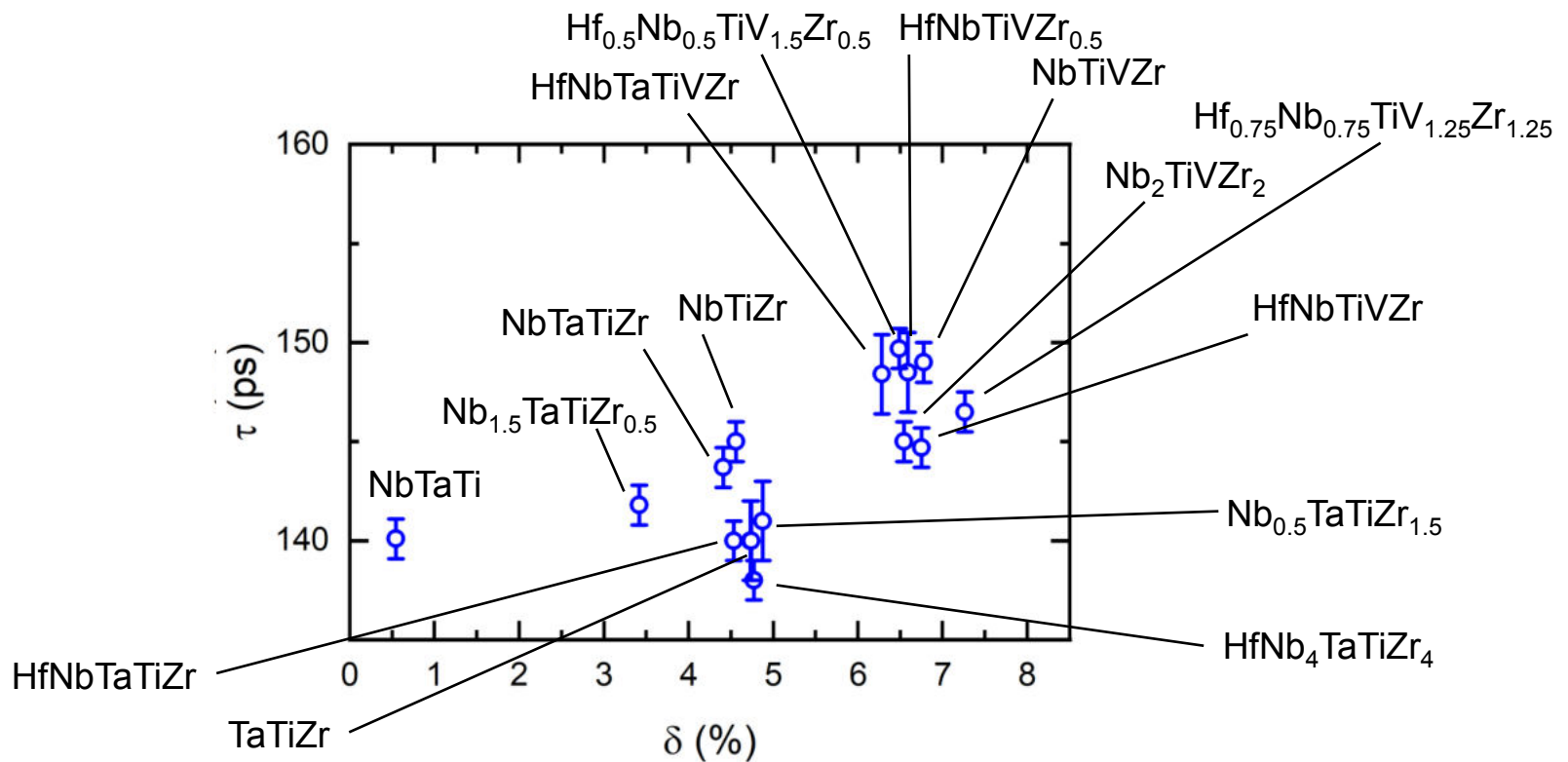
- mean positron lifetime  $\rightarrow$  single component fit of positron lifetime spectra
- as-cast alloys  $\rightarrow$  significant contribution of positrons trapped at dislocations
- alloys annealed in vacuum at 1200°C for 2 h  $\rightarrow$  positrons annihilated in the free state





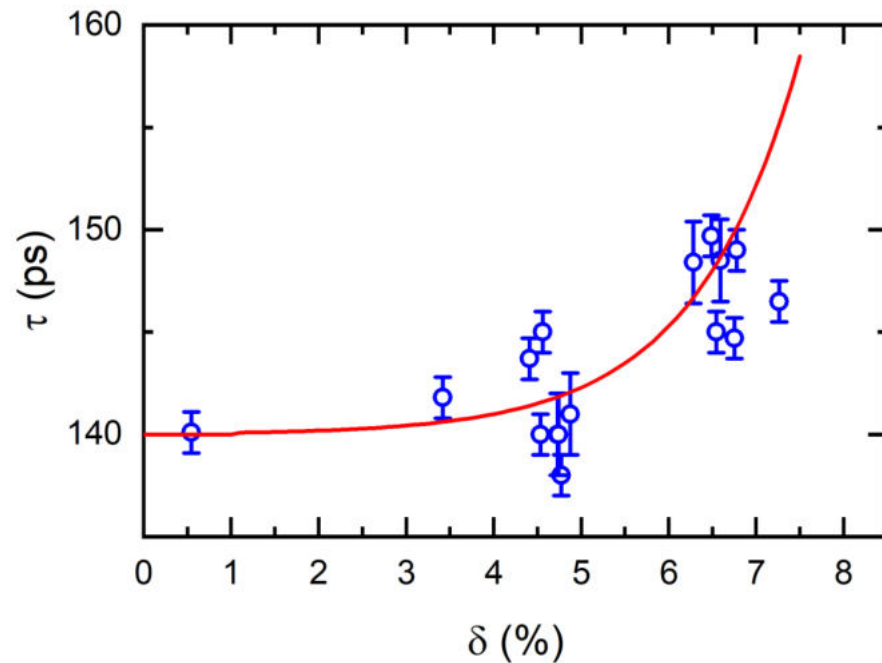
# Positron lifetime investigations of HEAs

- positron lifetimes of samples annealed in vacuum at 1200°C for 2 h



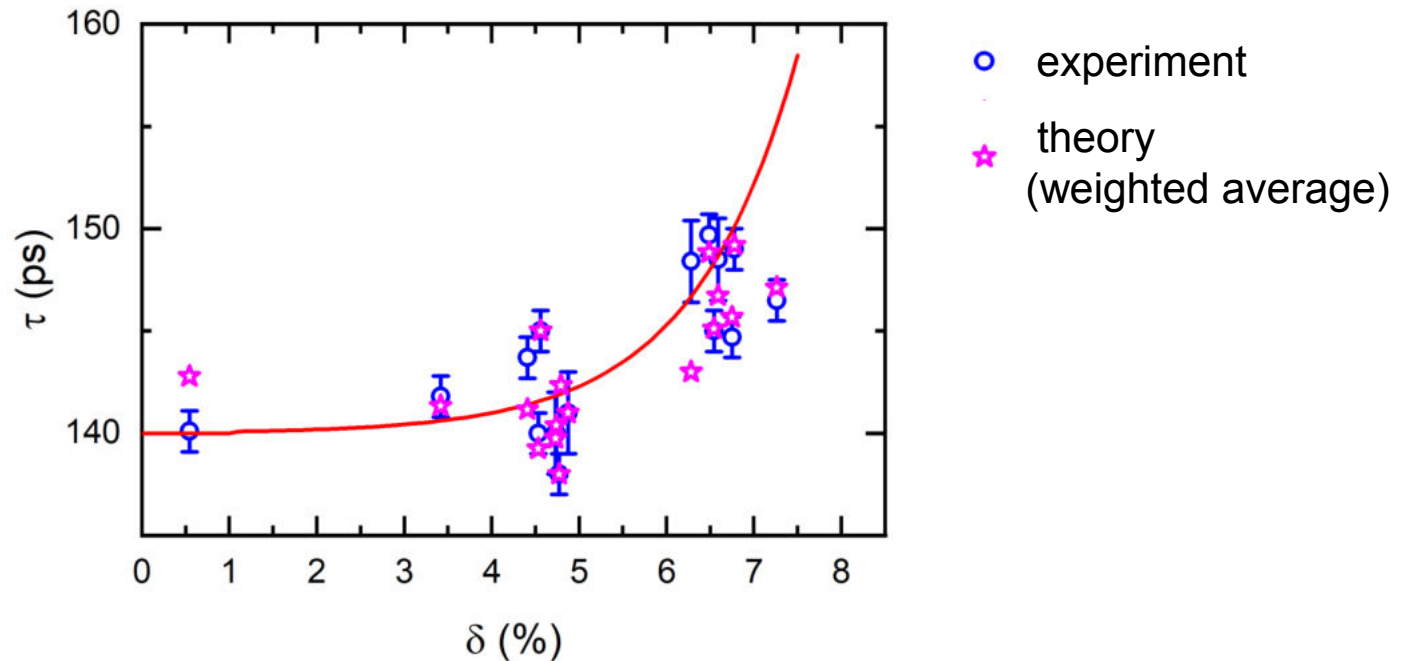
# Positron lifetime investigations of HEAs

- positron lifetimes of samples annealed in vacuum at 1200°C for 2 h
- **bulk positron lifetime increases with increasing magnitude of lattice distortions**



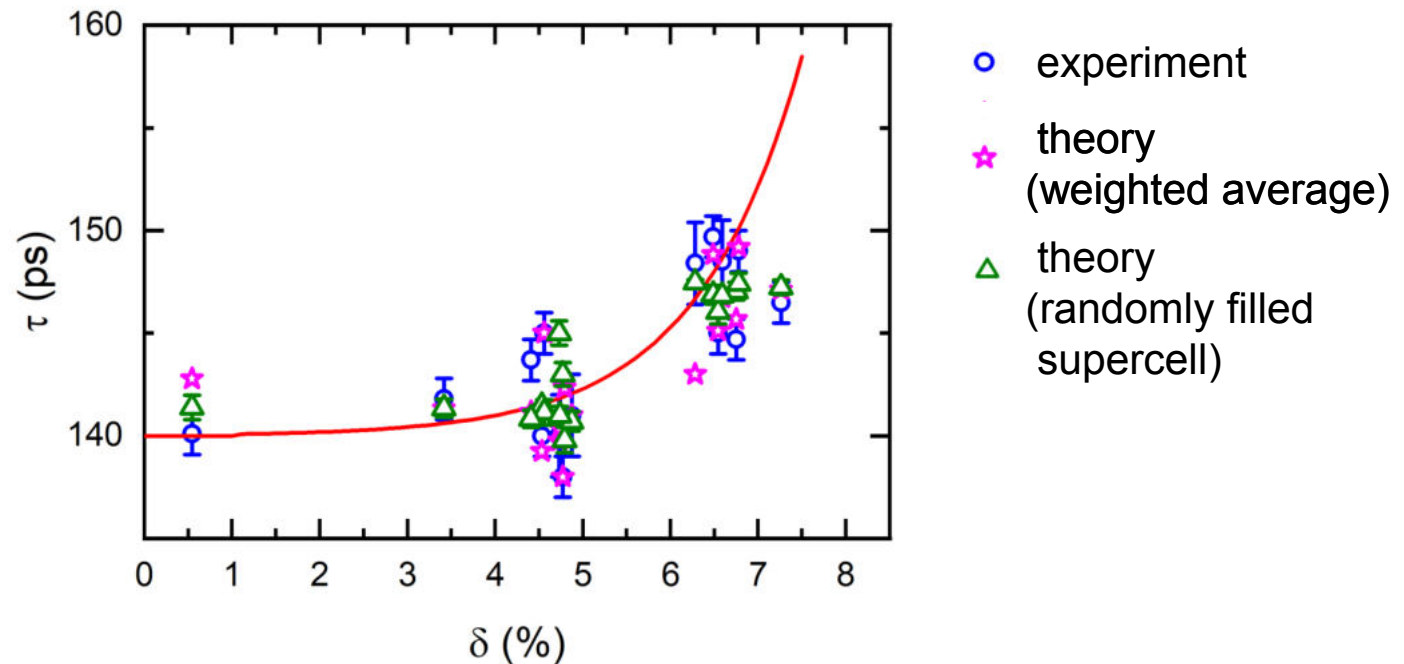
# Positron lifetime investigations of HEAs

- positron lifetimes of samples annealed in vacuum at 1200°C for 2 h
- **bulk positron lifetime increases with increasing magnitude of lattice distortions**



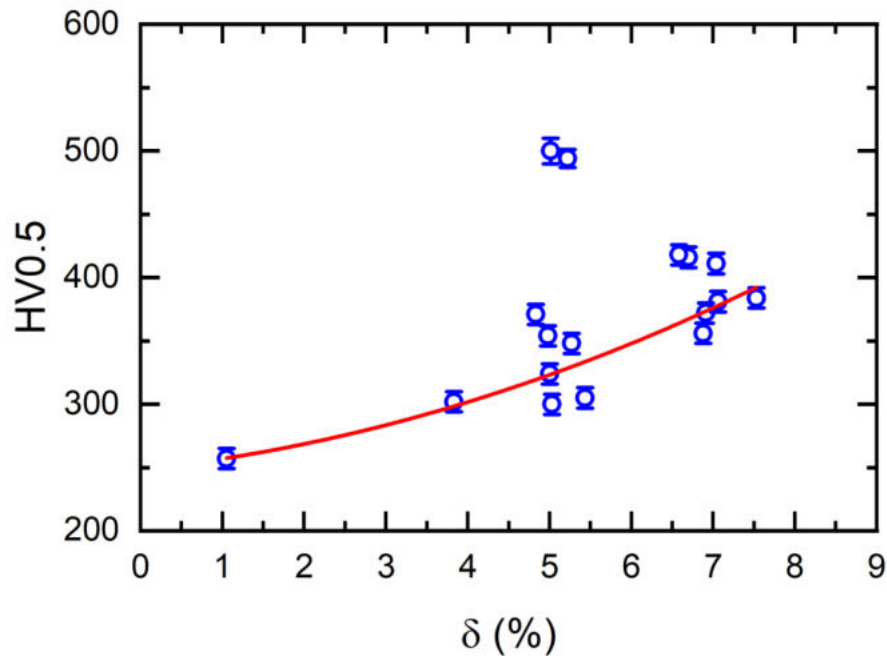
# Positron lifetime investigations of HEAs

- positron lifetimes of samples annealed in vacuum at 1200°C for 2 h
- **bulk positron lifetime increases with increasing magnitude of lattice distortions**



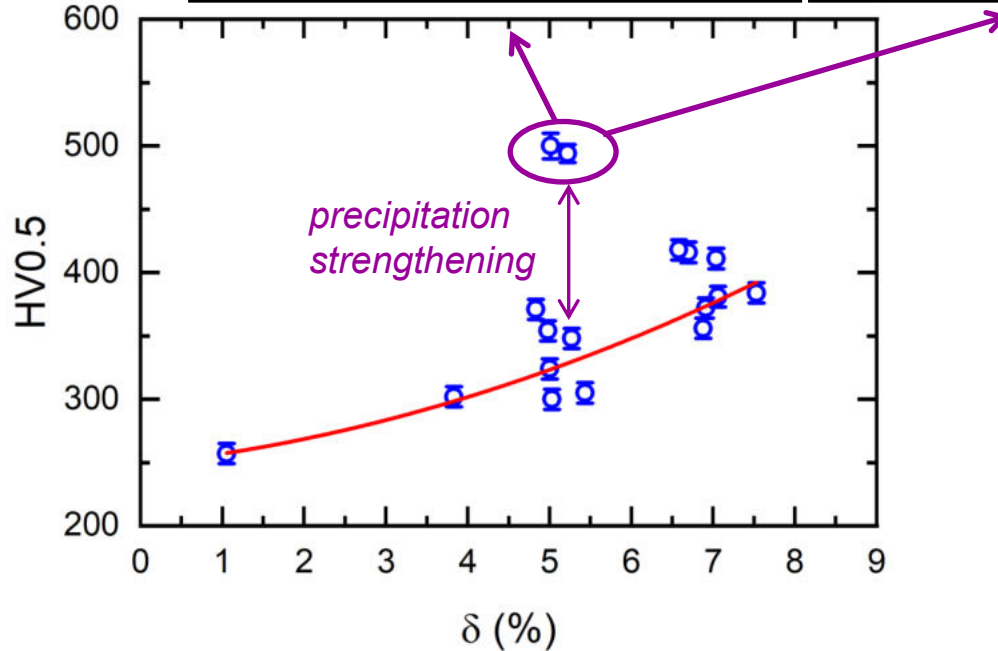
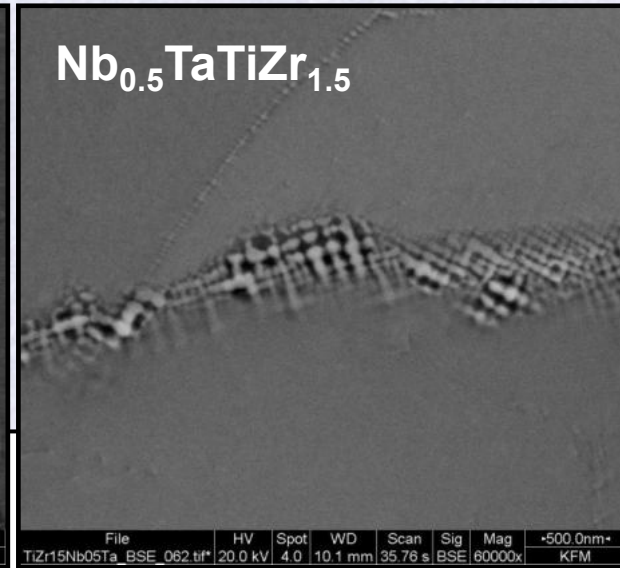
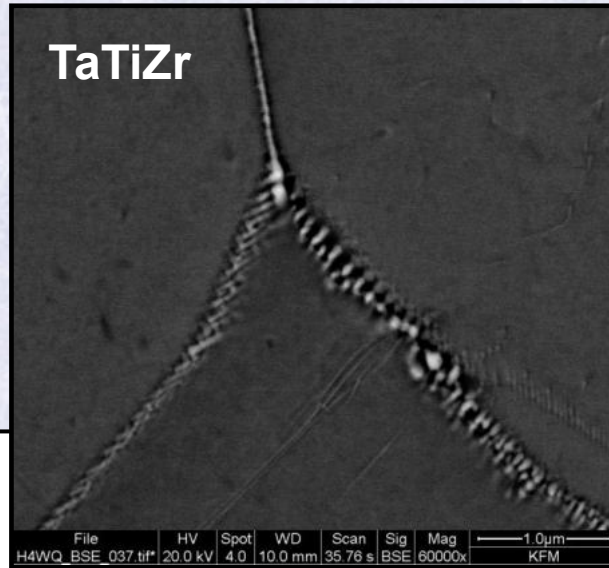
# Hardness of HEAs

- Vickers hardness (HV), load 0.5 kg applied for 10 s
- **hardness increases with increasing magnitude of lattice distortions**



# Hardness of HEAs

- additional precipitation strengthening
- Zr rich precipitates



# Conclusions

- The lattice distortion effect was examined in set of complex concentrated alloys of refractory metals Hf, Nb, Ta, Ti, V, Zr

- Positrons actively search for interstitial regions with extended open volume



- Bulk positron lifetime increases with increasing magnitude of lattice distortions



- Positron lifetime spectroscopy enables direct measurement of lattice distortions

- Lattice distortions cause strengthening of alloys

- Positive correlation between hardness and atomic misfit parameter  $\delta$  was observed

## Acknowledgements

- This work was supported by the Czech Science Agency (project 21-16218S)
- Computational resources were supplied by the project "e-Infrastruktura CZ" (e-INFRA LM2018140) provided within the program Projects of Large Research, Development and Innovations Infrastructures